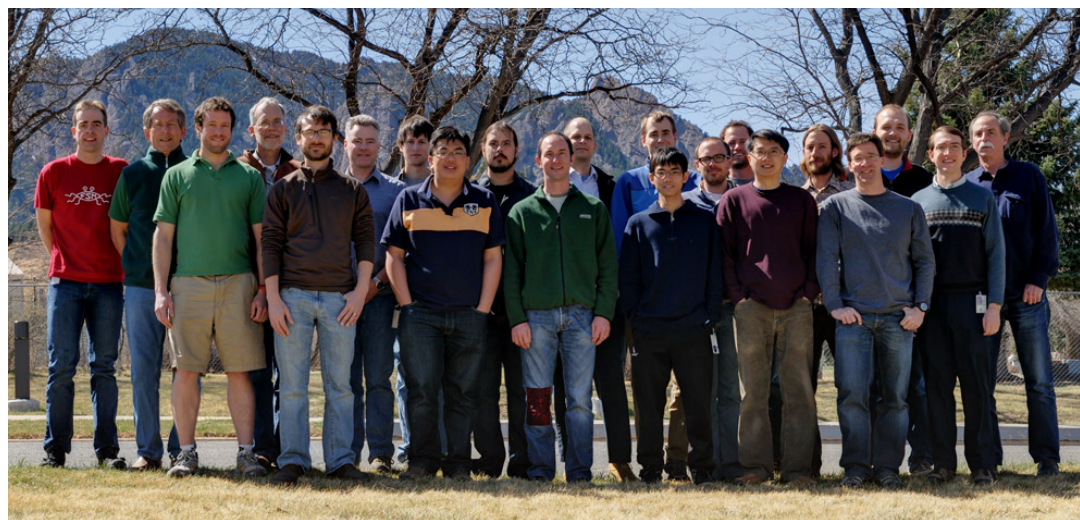


Trapped-ion metrology experiments at NIST



Ion Storage
Group
March 23, 2011

Jim Bergquist
Brad Blakestad (now JQI)
John Bollinger
Ryan Bowler
Joe Britton
Kenton Brown
James Chou
Yves Colombe
John Gaebler
David Hanneke (now at Amherst)
Dustin Hite
David Hume (now OFM)
Wayne Itano
Robert Jördens
John Jost
Dietrich Leibfried
Yiheng Lin
Christian Ospelkaus (now U Hannover)
Till Rosenband
Brian Sawyer
Ting-Rei Tan
Mike Thorpe
Ulrich Warring
Andrew Wilson
David Wineland

Efficient
Readout

Quantum Measurement (Ancilla-assisted readout):

- Readout of the Al^+ clock state

Multi-qubit
Control

Multi-qubit control:

- Entanglement and control with many ions in Penning traps

Entangled
States

Entangled States:

- Generation of entangled states with microwave field gradients (novel schemes)
- Coupled ion trap spectroscopy (novel systems and applications)

Theme – Shared ion motion due to strong Coulomb interaction used to generate entanglement and read out quantum states



NIST

Readout of the Al^+ clock state/ ancilla-assisted readout

Hume, Chou, Leibbrandt, Thorpe, Wineland, and Rosenband, arXiv:11085922v2

$${}^3P_0 \xrightarrow{\tau \simeq 20 \text{ s}} |\uparrow\rangle_{Al}$$

Al^+

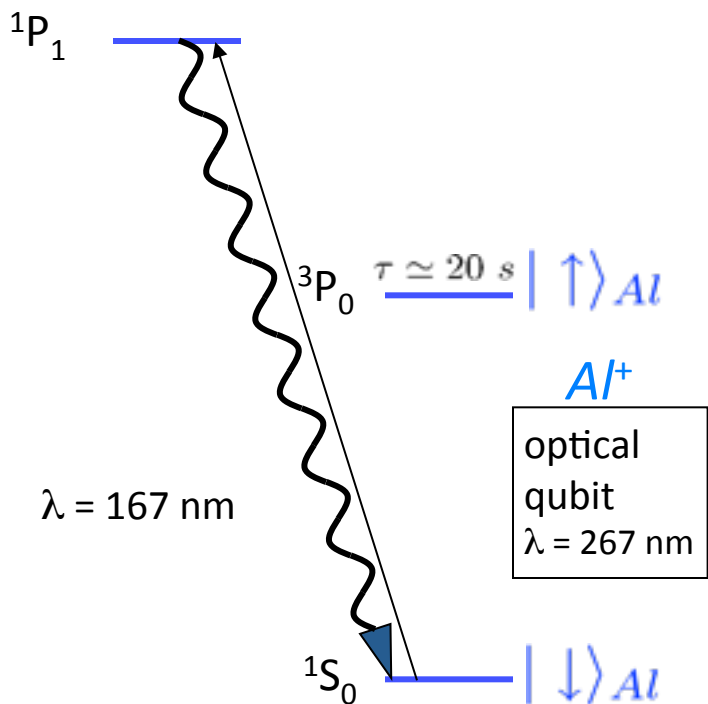
optical
qubit
 $\lambda = 267 \text{ nm}$

$${}^1S_0 \xrightarrow{\quad} |\downarrow\rangle_{Al}$$

$$\Psi = \alpha |{}^1S_0\rangle_{Al} + \beta |{}^3P_0\rangle_{Al}$$

Readout of the Al^+ clock state/ ancilla-assisted readout

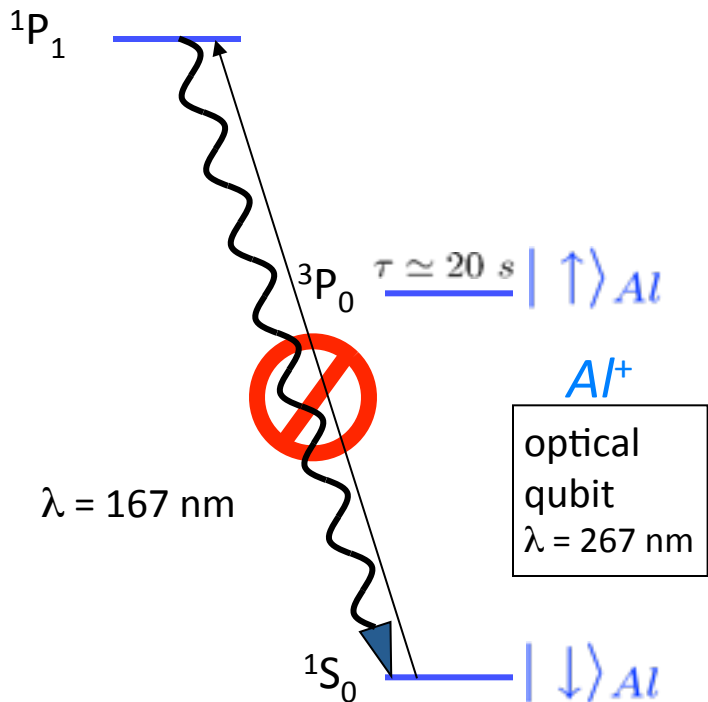
Hume, Chou, Leibbrandt, Thorpe, Wineland, and Rosenband, arXiv:11085922v2



$$\Psi = \alpha|1S_0\rangle_{Al} + \beta|3P_0\rangle_{Al}$$

Readout of the Al^+ clock state/ ancilla-assisted readout

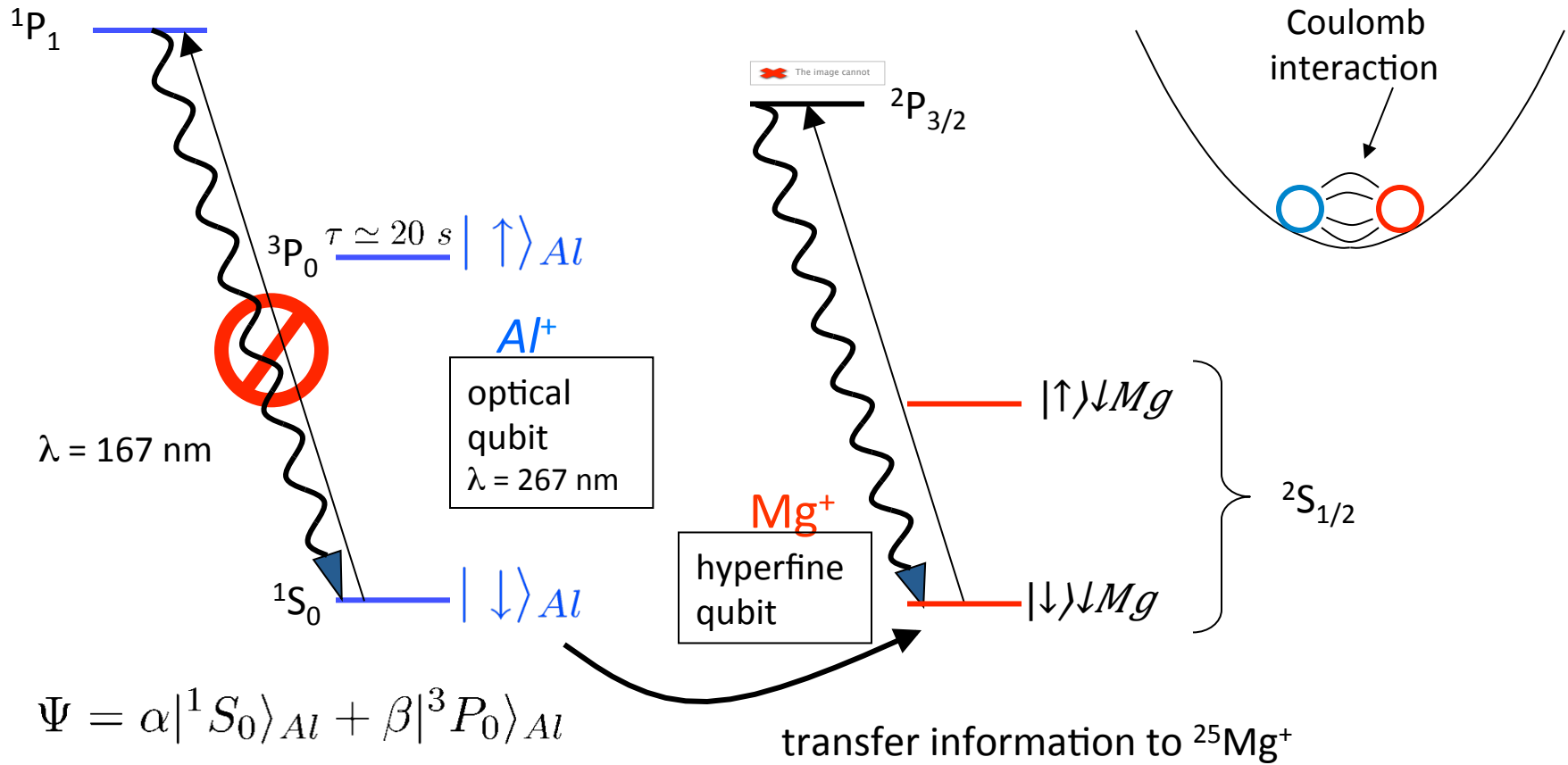
Hume, Chou, Leibbrandt, Thorpe, Wineland, and Rosenband, arXiv:11085922v2



$$\Psi = \alpha|1S_0\rangle_{Al} + \beta|3P_0\rangle_{Al}$$

Readout of the Al^+ clock state/ ancilla-assisted readout

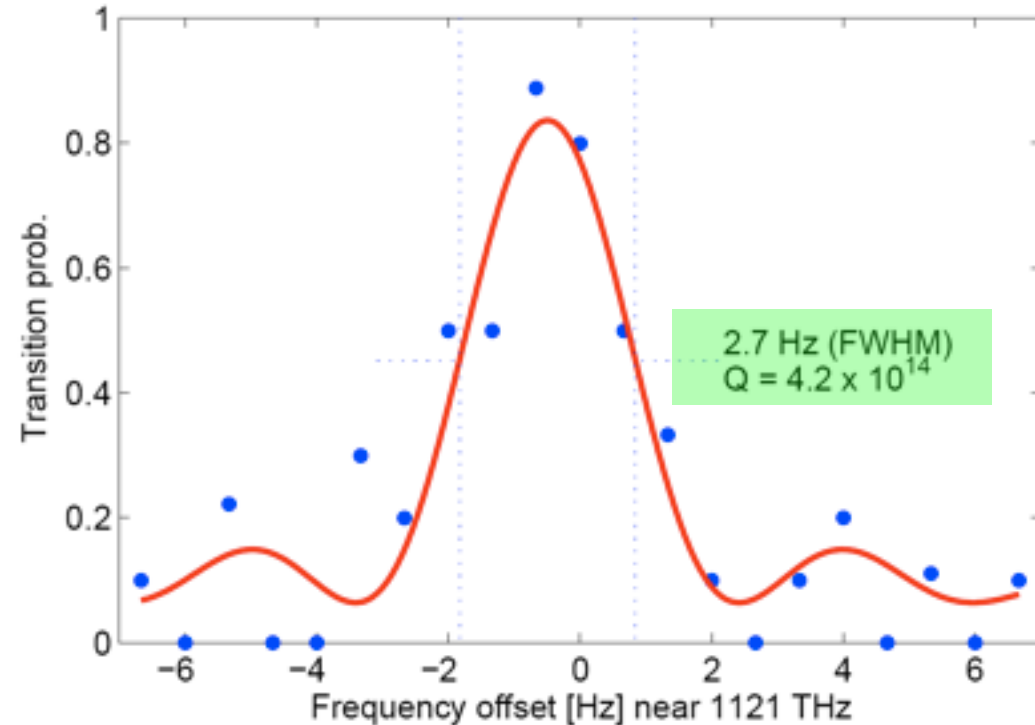
Hume, Chou, Leibrandt, Thorpe, Wineland, and Rosenband, arXiv:11085922v2



Readout of the Al⁺ clock state/ ancilla-assisted readout

Hume, Chou, Leibbrandt, Thorpe, Wineland, and Rosenband, arXiv:11085922v2

Al⁺ ¹S₀ - ³P₀ resonance (10 scans, 300 ms probe time)

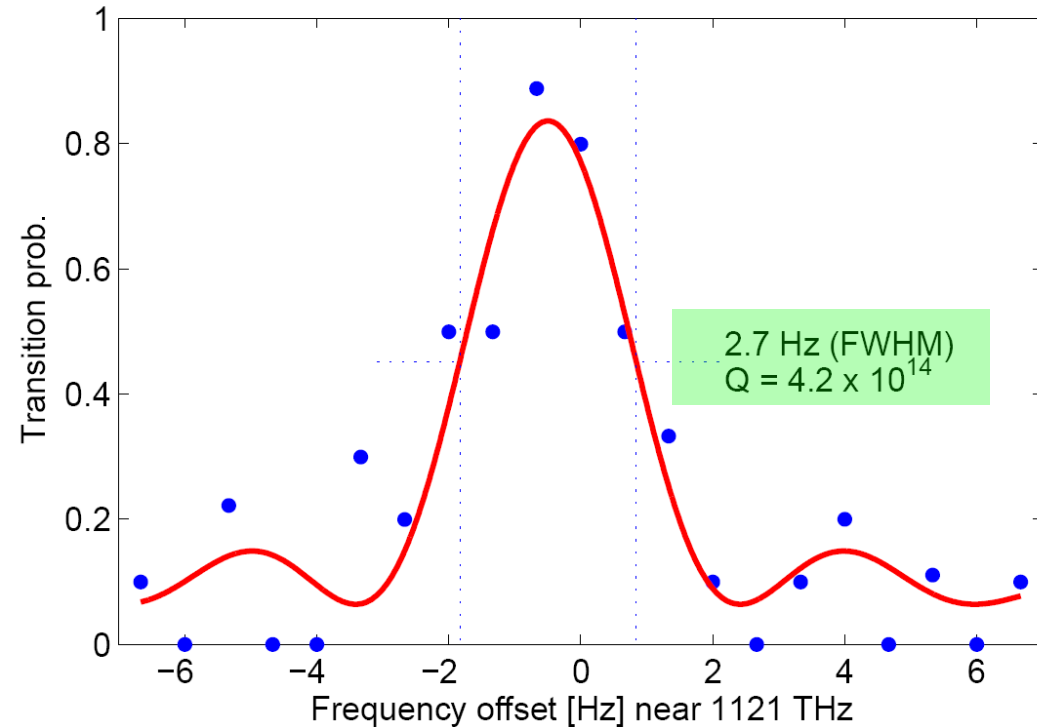


- Insensitive to external fields
- Smallest known temperature sensitivity (10^{-19} / Kelvin)
- current evaluated inaccuracy 0.9×10^{-17}
- Hg⁺/Al⁺ comparison places limit $\frac{\dot{\alpha}}{\alpha} < 3 \times 10^{-17}/\text{yr}$
- Measure time dilation due to 1 m change in height
- Potential applications in geodesy/geophysics

Readout of the Al⁺ clock state/ ancilla-assisted readout

Hume, Chou, Leibrandt, Thorpe, Wineland, and Rosenband, arXiv:11085922v2

Al⁺ ¹S₀ - ³P₀ resonance (10 scans, 300 ms probe time)



- Insensitive to external fields
- Smallest known temperature sensitivity (10^{-19} / Kelvin)
- current evaluated inaccuracy 0.9×10^{-17}
- Hg⁺/Al⁺ comparison places limit $\alpha / \alpha < 3 \times 10^{-17}/\text{yr}$
- Measure time dilation due to 1 m change in height
- Potential applications in geodesy/ geophysics

Current effort: move the Al⁺ clock out of the lab

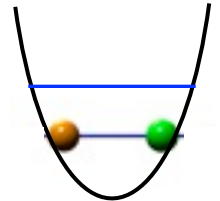
Trapped-Ion State Detection through Coherent Motion

Simplified readout:

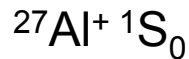
D. B. Hume,* C. W. Chou, D. R. Leibrandt, M. J. Thorpe, D. J. Wineland, and T. Rosenband
Time and Frequency Division, National Institute of Standards and Technology, Boulder, Colorado 80305
(Dated: September 7, 2011)

arXiv:1108.5922v2
To appear in PRL

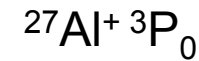
Al⁺ quantum-logic spectroscopy



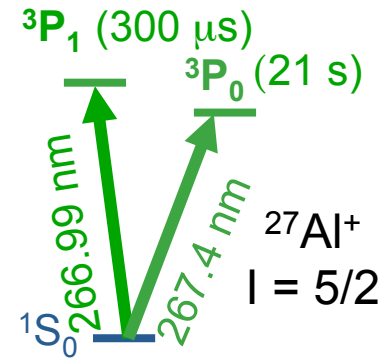
1. Cool to motional ground-state with Mg⁺ (Raman cooling)
2. Depending on Al⁺ clock state, add one vibrational quantum via 1S_0 - 3P_1
3. Detect vibrational quantum with Mg⁺



Mean = 1.3



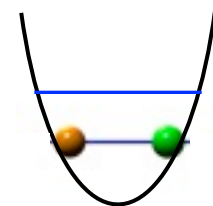
Mean = 6.9



Probability

Mg⁺ photon counts

Al⁺ quantum-logic spectroscopy



QND

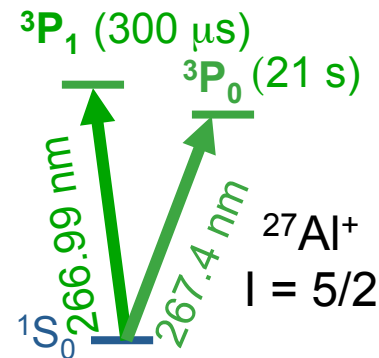
1. Cool to motional ground-state with Mg⁺ (Raman cooling)
2. Depending on Al⁺ clock state, add one vibrational quantum via 1S_0 - 3P_1
3. Detect vibrational quantum with Mg⁺

$^{27}\text{Al}^+ \ ^1S_0$

Mean = 1.3

$^{27}\text{Al}^+ \ ^3P_0$

Mean = 6.9



Probability

99.94% Detection fidelity

Mg⁺ photon counts

P.O. Schmidt, *et al.*
Science **309**, 749 (2005)

D. B. Hume, *et al.*
PRL **99**, 120502 (2007)

~~Al⁺ quantum-logic spectroscopy~~

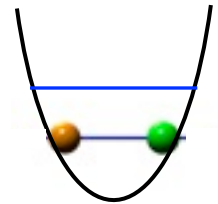
QND



1. Cool to motional ground-state with Mg⁺ (Raman cooling)
2. Depending on Al⁺ clock state, add one vibrational quantum via 1S_0 - 3P_1
3. Detect vibrational quantum with Mg⁺

$^{27}\text{Al}^+ \ ^1S_0$
Mean = 1.3

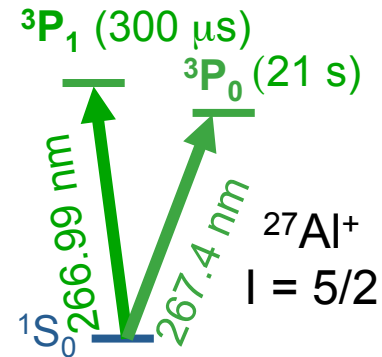
$^{27}\text{Al}^+ \ ^3P_0$
Mean = 6.9



D. B. Hume, *et al.*
PRL (accepted)


Probability

99.94% Detection fidelity



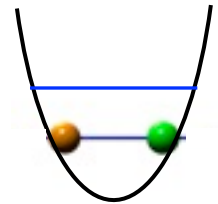
Mg⁺ photon counts

Al⁺ coherent-drive spectroscopy

- QND
- 
1. Cool to motional ground-state with Mg⁺ (Raman cooling)
 2. Depending on Al⁺ clock state, add one vibrational quantum via 1S_0 - 3P_1
 3. Detect vibrational quantum with Mg⁺

$^{27}\text{Al}^+ \ ^1S_0$
Mean = 1.3

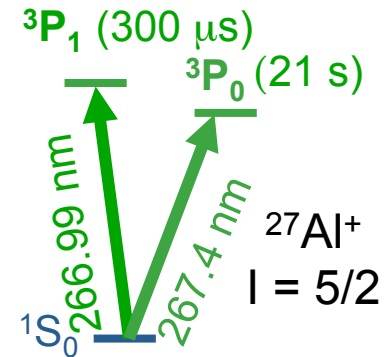
$^{27}\text{Al}^+ \ ^3P_0$
Mean = 6.9



D. B. Hume, *et al.*
PRL (accepted)

Probability

99.94% Detection fidelity



Mg⁺ photon counts

Al⁺ coherent-drive spectroscopy

Mg⁺ Doppler

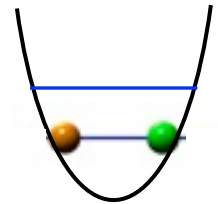
- ~~Cool to motional ground state with Mg⁺ (Raman cooling)~~
- Depending on Al⁺ clock state, add one vibrational quantum via 1S_0 - 3P_1
- Detect vibrational quantum with Mg⁺

QND



$^{27}\text{Al}^+ \ ^1S_0$
Mean = 1.3

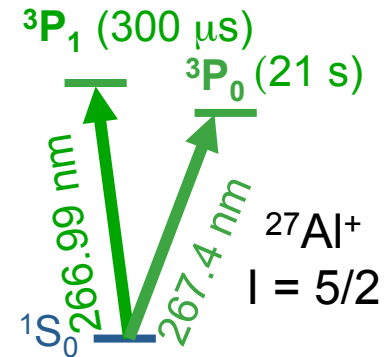
$^{27}\text{Al}^+ \ ^3P_0$
Mean = 6.9



D. B. Hume, *et al.*
PRL (accepted)

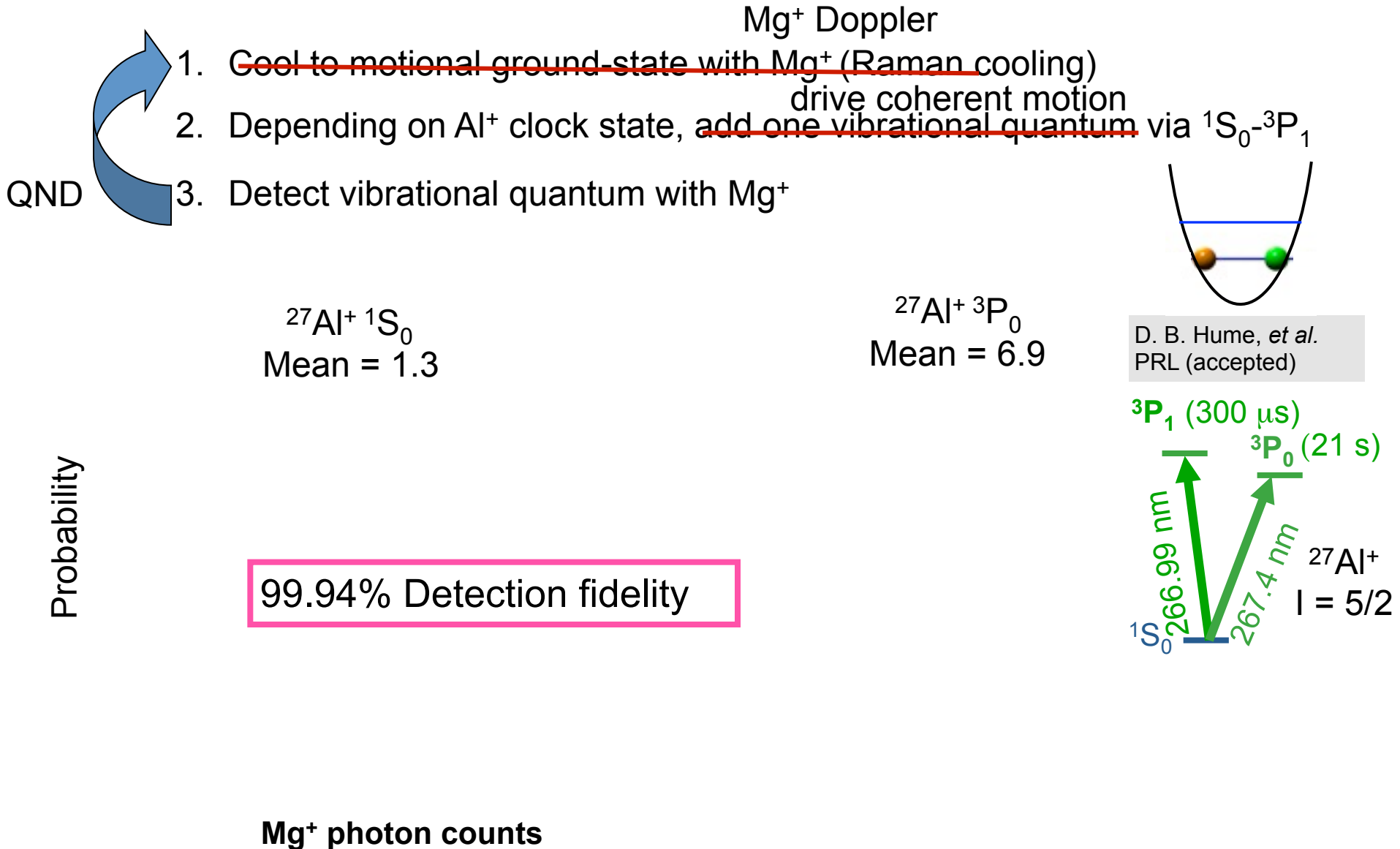
Probability

99.94% Detection fidelity



Mg⁺ photon counts

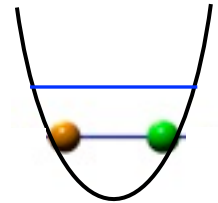
Al⁺ coherent-drive spectroscopy



Al⁺ coherent-drive spectroscopy

Mg⁺ Doppler

- ~~Cool to motional ground state with Mg⁺ (Raman cooling)~~
- Depending on Al⁺ clock state, ~~add one vibrational quantum~~ drive coherent motion via 1S_0 - 3P_1
- Detect ~~vibrational quantum~~ with Mg⁺ coherent motion



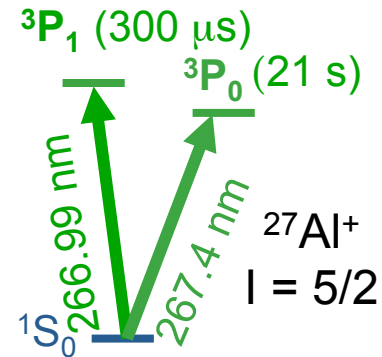
$^{27}\text{Al}^+ \ ^1S_0$
Mean = 1.3

$^{27}\text{Al}^+ \ ^3P_0$
Mean = 6.9

D. B. Hume, *et al.*
PRL (accepted)

Probability

99.94% Detection fidelity



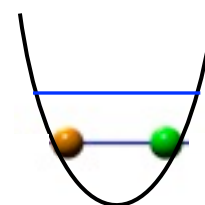
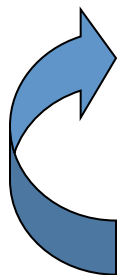
Mg⁺ photon counts

Al⁺ coherent-drive spectroscopy

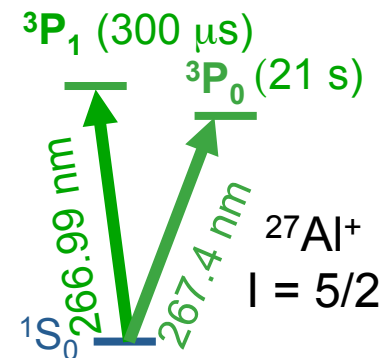
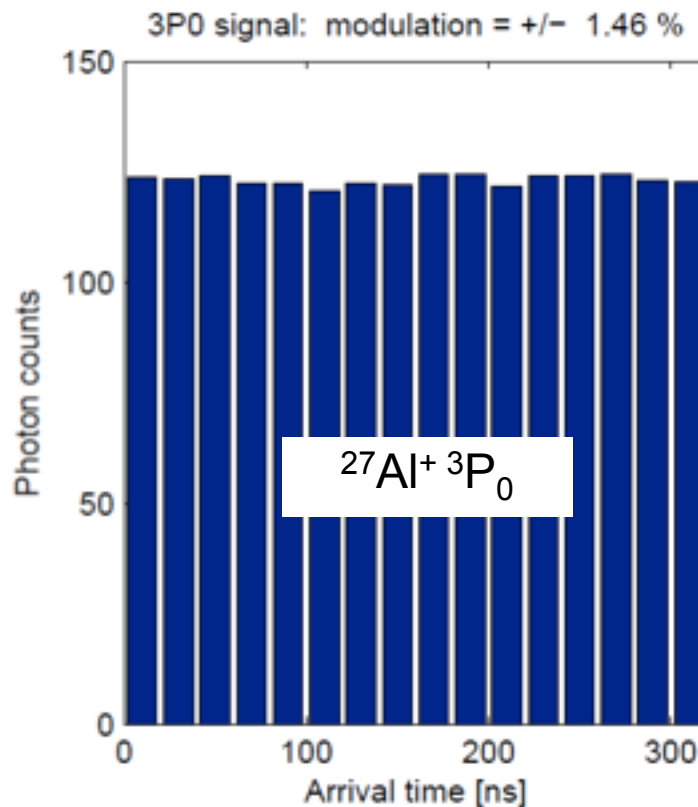
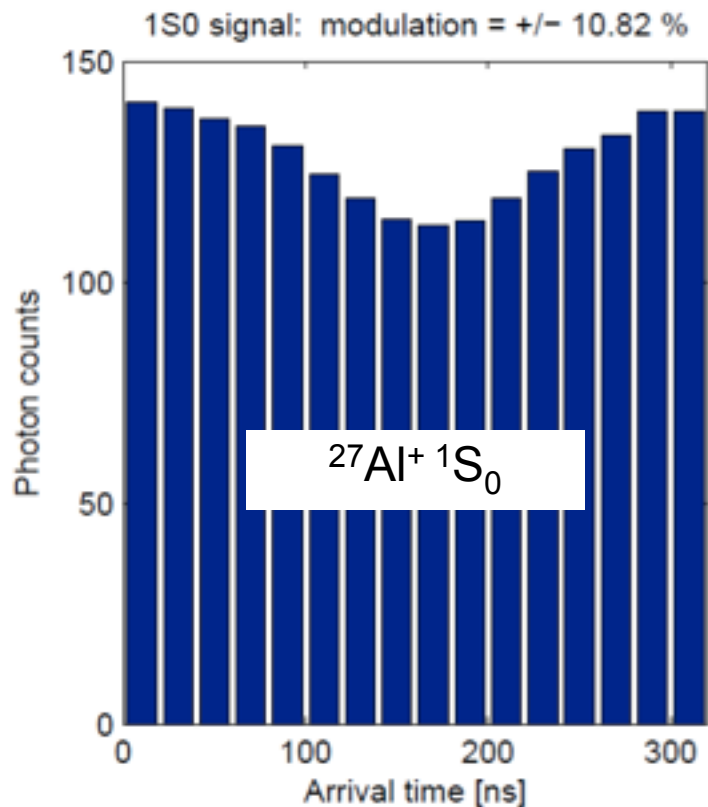
Mg⁺ Doppler

- ~~Cool to motional ground state with Mg⁺ (Raman cooling)~~
- Depending on Al⁺ clock state, ~~add one vibrational quantum~~ drive coherent motion via 1S_0 - 3P_1
- Detect ~~vibrational quantum~~ with Mg⁺ coherent motion

QND



D. B. Hume, *et al.*
PRL (accepted)

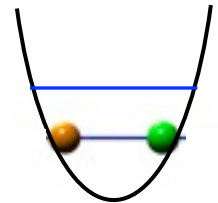


Al⁺ coherent-drive spectroscopy

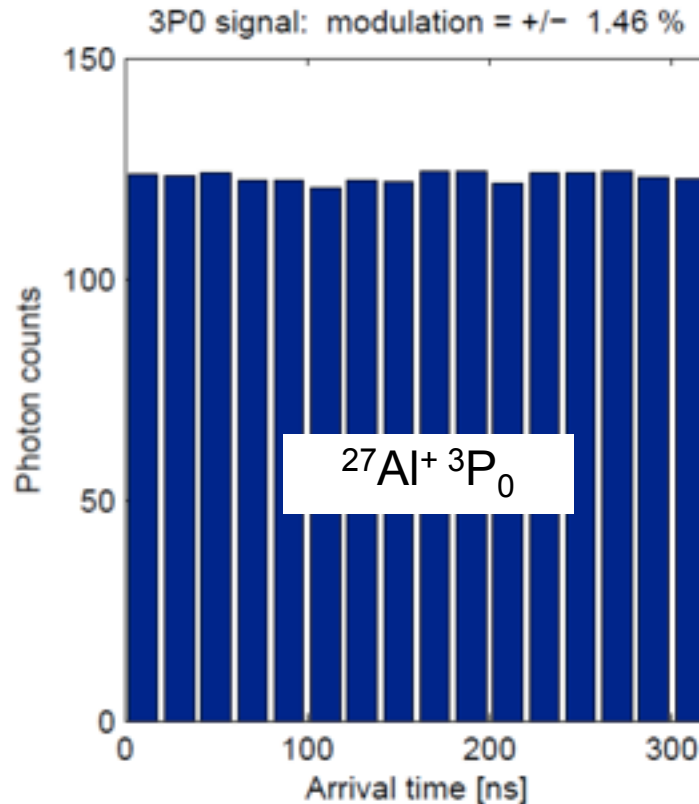
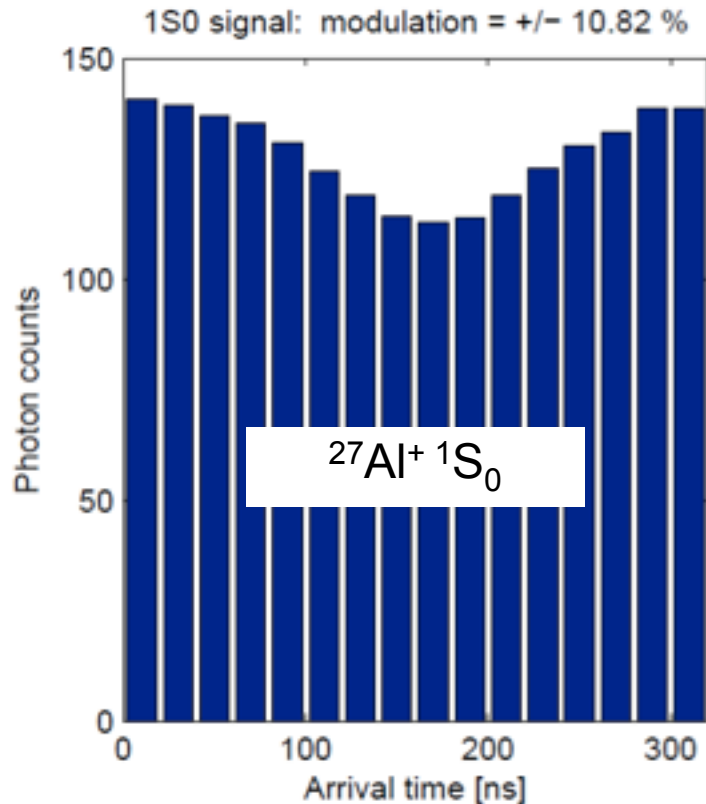
Mg⁺ Doppler

- ~~Cool to motional ground state with Mg⁺ (Raman cooling)~~
- Depending on Al⁺ clock state, ~~add one vibrational quantum~~ drive coherent motion via 1S_0 - 3P_1
- Detect ~~vibrational quantum~~ with Mg⁺ coherent motion

QND



D. B. Hume, *et al.*
PRL (accepted)



Measure quantum state w/o scattering photons

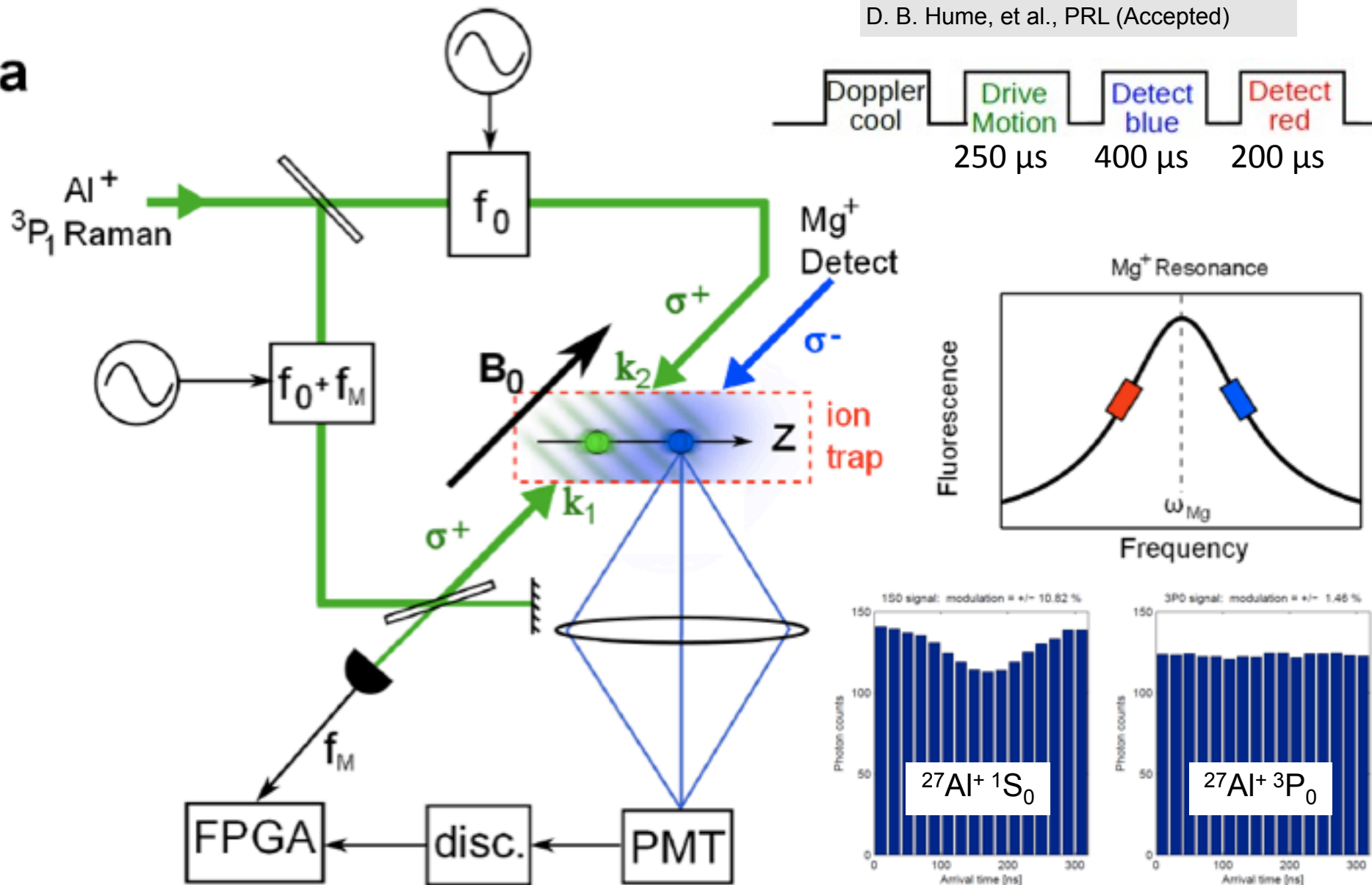
Simplified lasers (no ground-state cooling)

Slower

Al⁺ coherent-drive spectroscopy

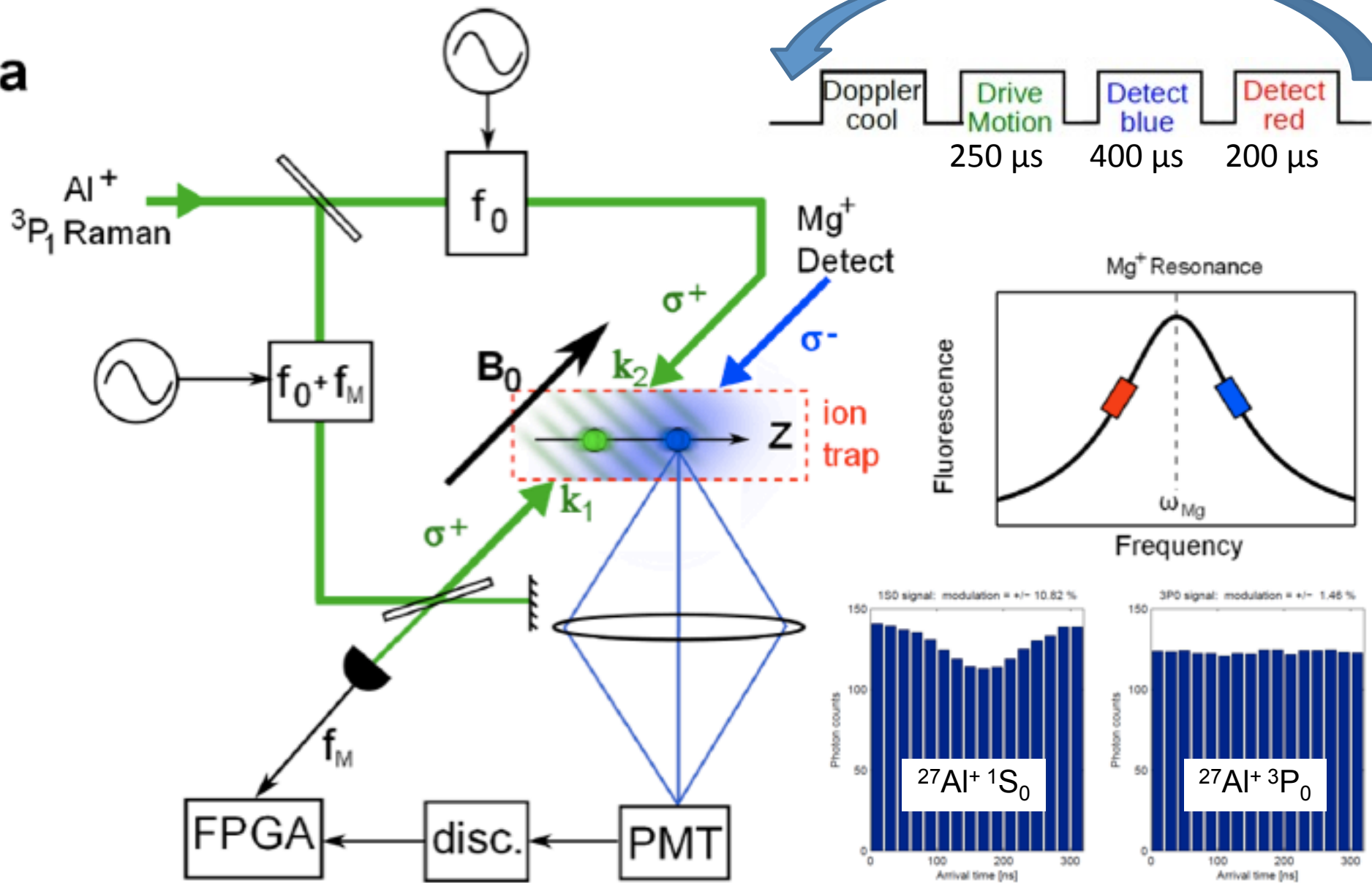
D. B. Hume, et al., PRL (Accepted)

a



Al⁺ coherent-drive spectroscopy

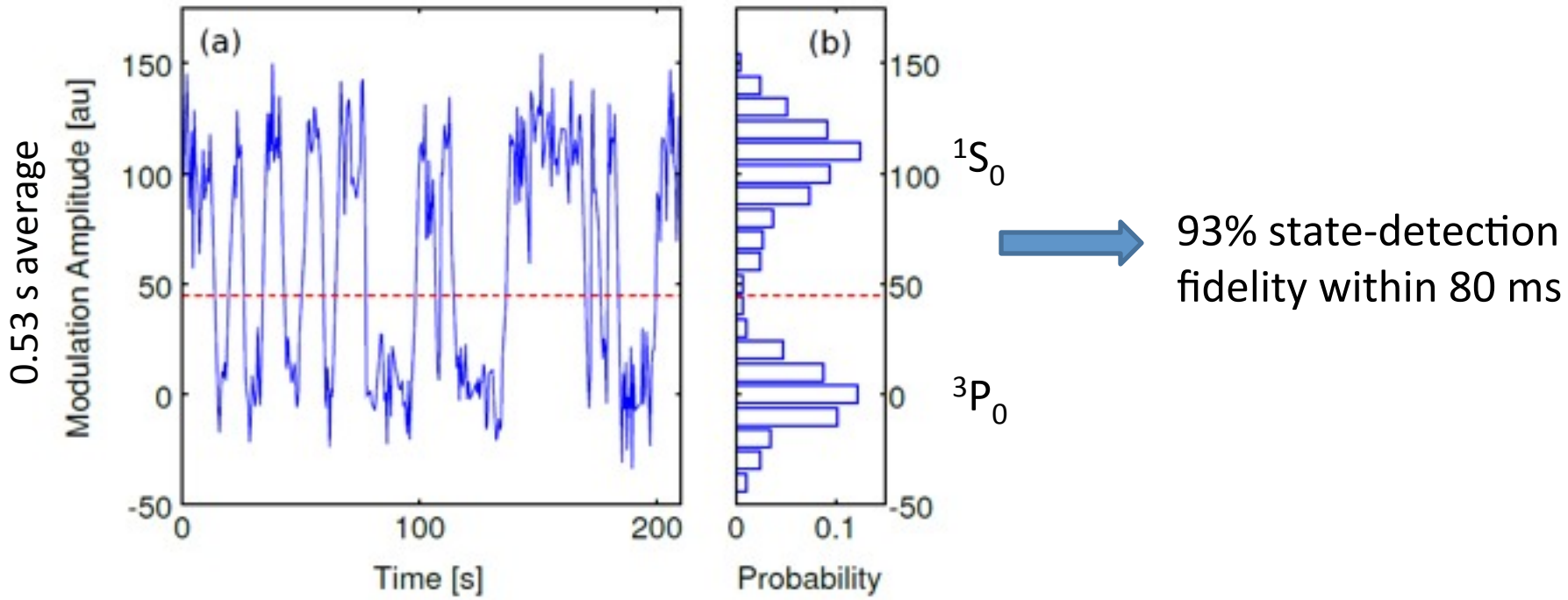
a



Readout of the Al^+ clock state/ ancilla-assisted readout

Hume, Chou, Leibbrandt, Thorpe, Wineland, and Rosenband, arXiv:11085922v2

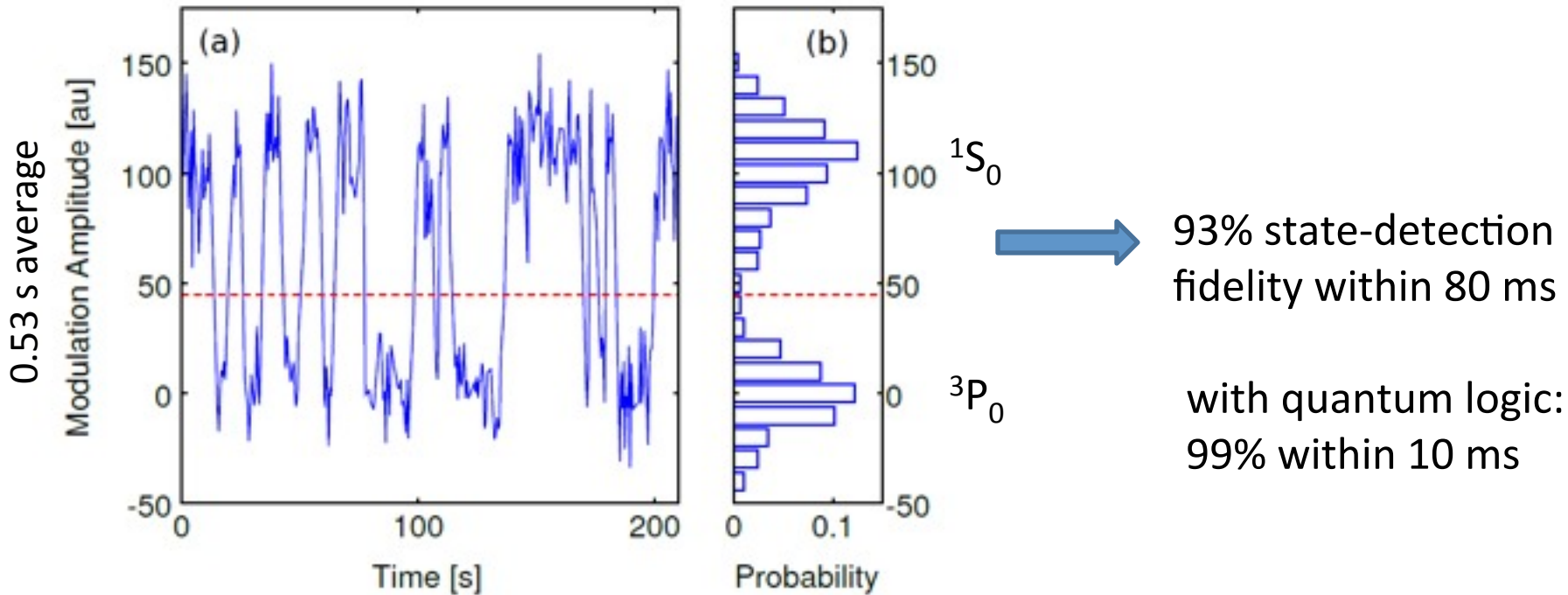
Quantum jumps between clock states ($^1\text{S}_0$ and $^3\text{P}_0$)



Readout of the Al^+ clock state/ ancilla-assisted readout

Hume, Chou, Leibbrandt, Thorpe, Wineland, and Rosenband, arXiv:11085922v2

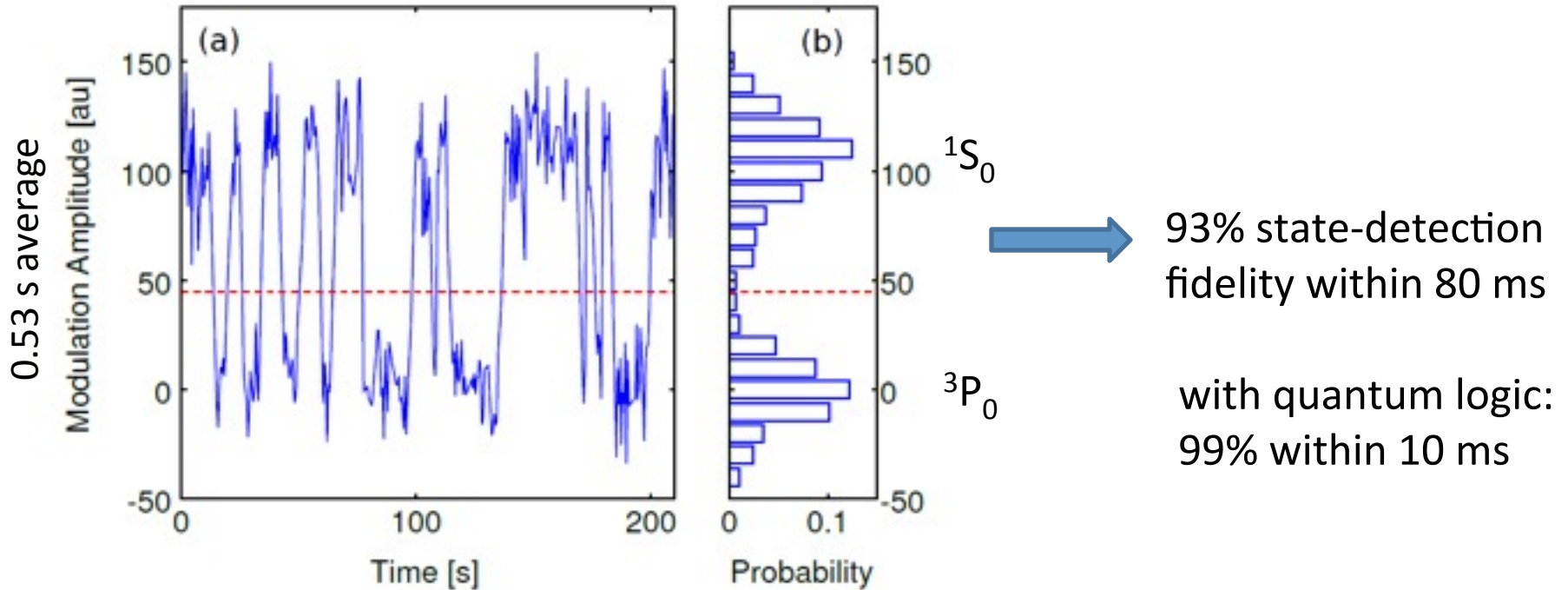
Quantum jumps between clock states ($^1\text{S}_0$ and $^3\text{P}_0$)



Readout of the Al⁺ clock state/ ancilla-assisted readout

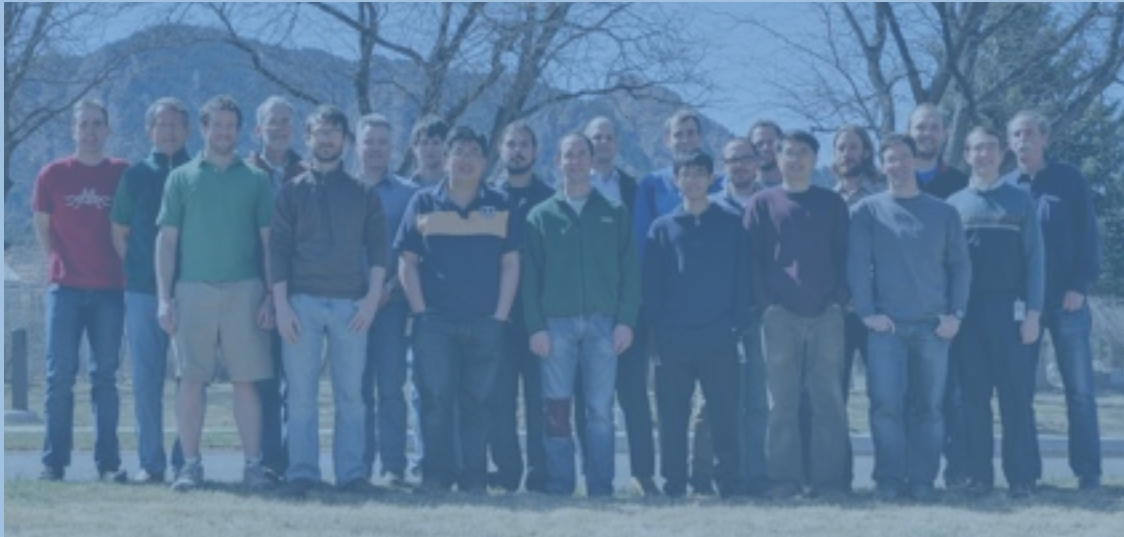
Hume, Chou, Leibbrandt, Thorpe, Wineland, and Rosenband, arXiv:11085922v2

Quantum jumps between clock states (1S_0 and 3P_0)



- coherent drive detection rate could be improved by higher modulation amplitude or photon collection efficiency
- can be generalized for more than one Al⁺ ion

Trapped-ion metrology experiments at NIST



Ion Storage
Group
March 23, 2011

Jim Bergquist
Brad Blakestad (now JQI)
John Bollinger
Ryan Bowler
Joe Britton
Kenton Brown
James Chou
Yves Colombe
John Gaebler
David Hanneke (now at Amherst)
Dustin Hite
David Hume (now OFM)
Wayne Itano
Robert Jördens
John Jost
Dietrich Leibfried
Yiheng Lin
Christian Ospelkaus (now U Hannover)
Till Rosenband
Brian Sawyer
Ting-Rei Tan
Mike Thorpe
Ulrich Warring
Andrew Wilson
David Wineland

Quantum Measurement (Ancilla-assisted readout):

- Readout of the Al^+ clock state

Multi-qubit control:

- Entanglement and control with many ions in Penning traps

Entangled States:

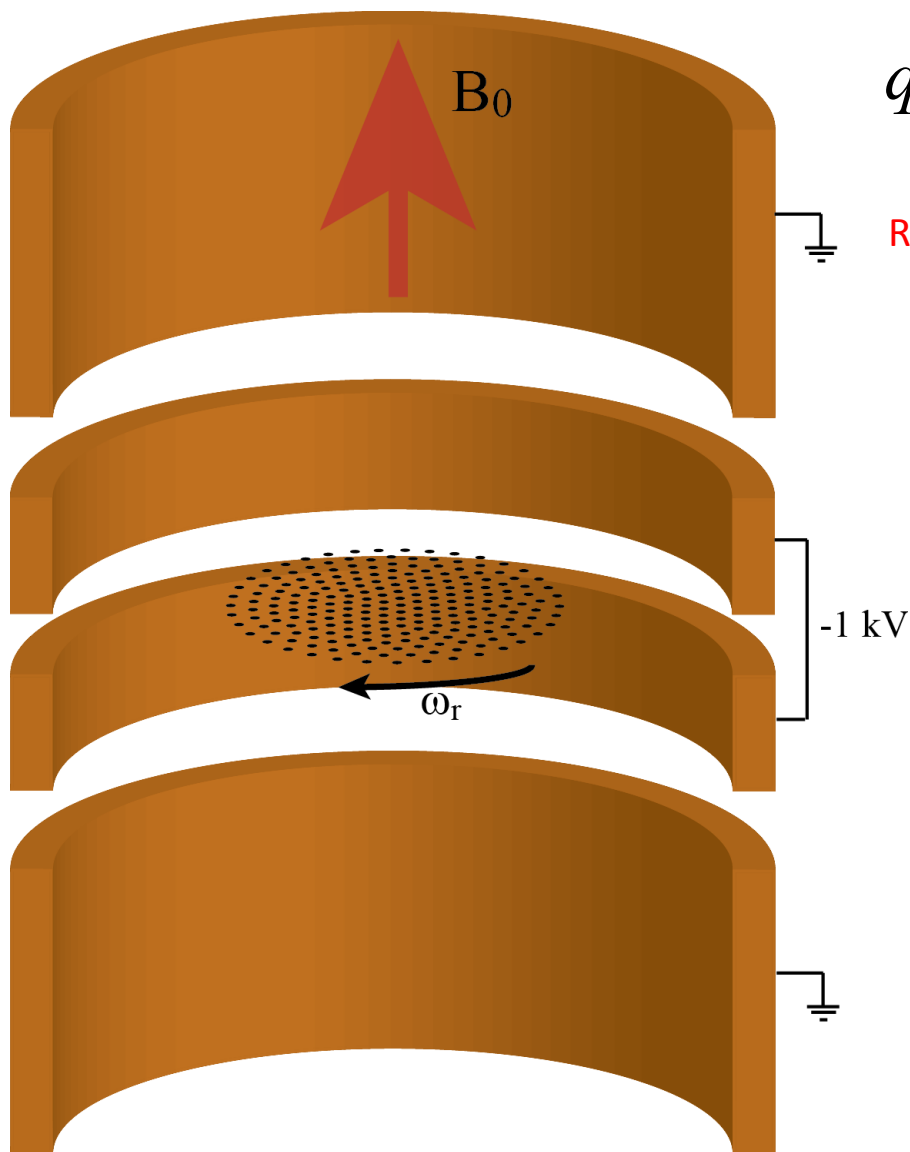
- Generation of entangled states with microwave field gradients (novel schemes)
- Coupled ion trap spectroscopy (novel systems and applications)

Theme – Shared ion motion due to strong Coulomb interaction used to generate entanglement and read out quantum states



Multi-qubit control - Entanglement and control with many ions in Penning traps

Britton, Sawyer, Bollinger/work supported by DARPA OLE



trap axial frequency

$$q\Phi_{\text{trap}}(r, z) = \frac{1}{2} m \omega_z^2 \left(z^2 + \beta(\omega_r) r^2 \right)$$

cyclotron frequency

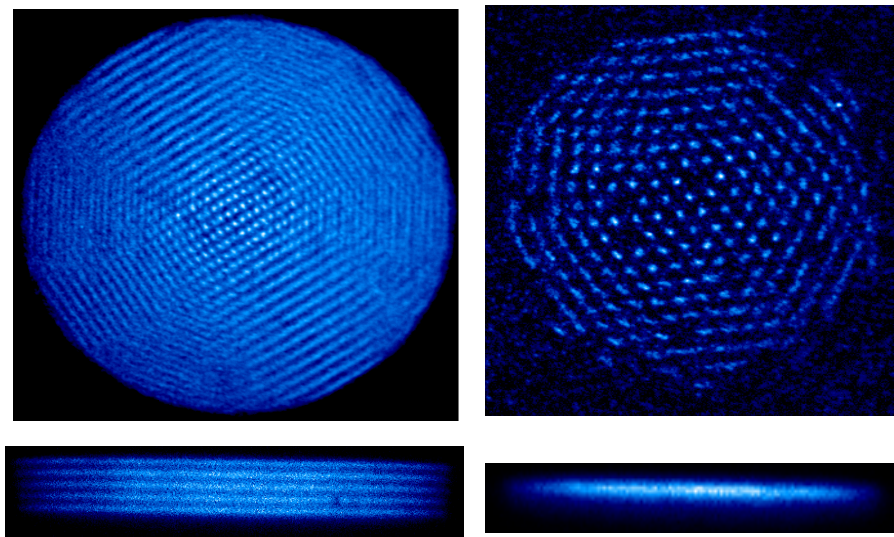
Radial confinement by rotation through the B_0 field

$$\beta \equiv \frac{\omega_r (\Omega_c - \omega_r)}{\omega_z^2} - \frac{1}{2}$$

$$\omega \downarrow r \approx 2\pi \times 45 \text{ kHz}$$

$$\omega \downarrow z \approx 2\pi \times 800 \text{ kHz}$$

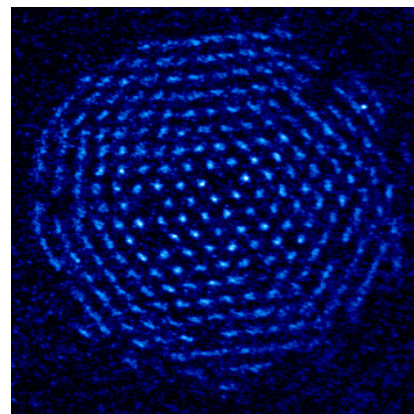
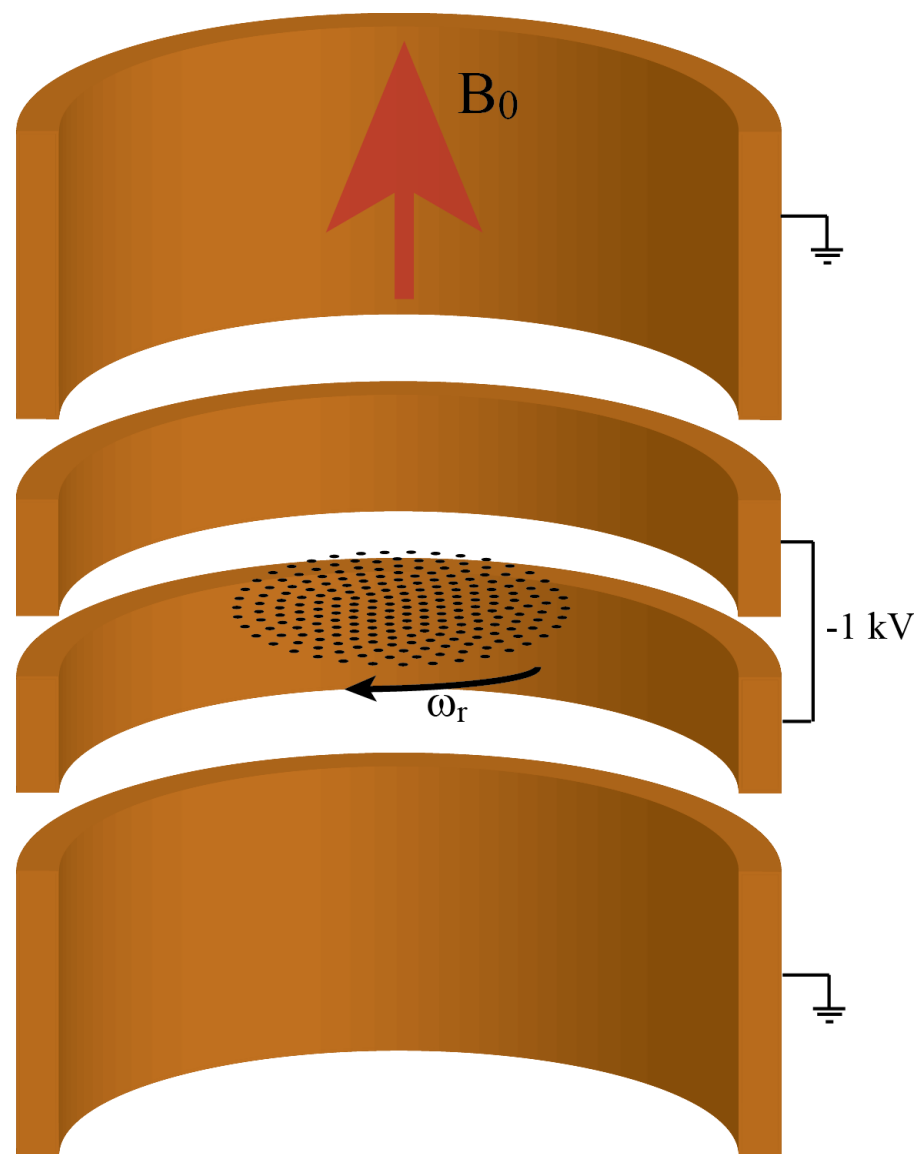
$$\Omega \downarrow c \approx 2\pi \times 7.6 \text{ MHz}$$



$T \lesssim 1 \text{ mK}$

Multi-qubit control - Entanglement and control with many ions in Penning traps

Britton, Sawyer, Bollinger/work supported by DARPA OLE



$$H_{\text{Ising}} = \frac{1}{N} \sum_{i < j} J_{i,j} \sigma_i^z \sigma_j^z$$

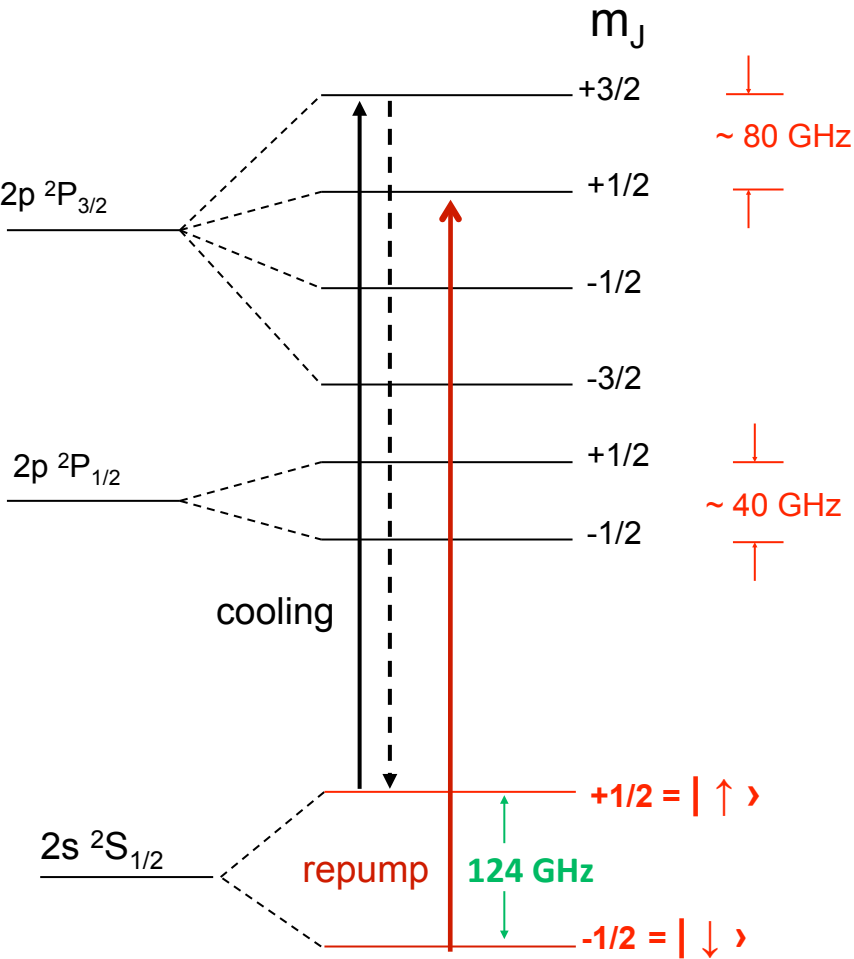
current effort: engineer spin-spin interactions for simulation of quantum magnetism

potential QuISM MURI interest: engineered spin-spin interactions should generate entanglement

Penning trap provides well controlled environment for measuring entanglement and studying techniques such as DD for extending the entanglement lifetime.

High magnetic field Be^+ qubit

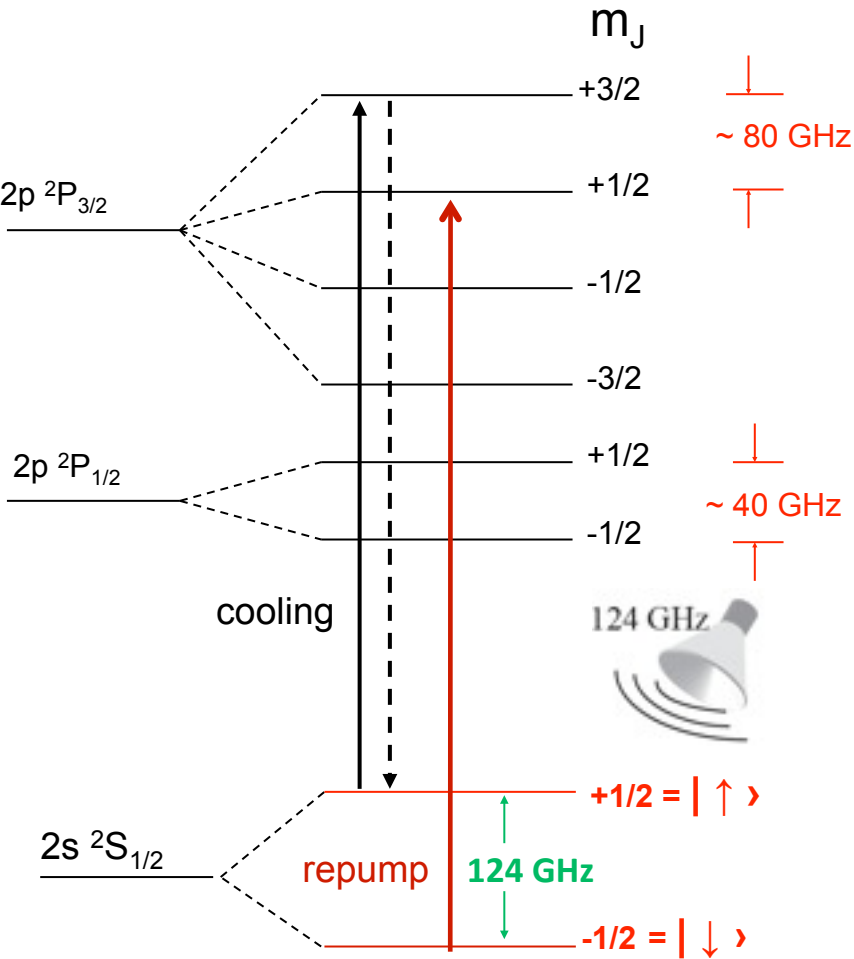
$^9\text{Be}^+$, $B \sim 4.6 \text{ T}$, $\omega_0 / 2\pi \sim 124.1 \text{ GHz}$



High magnetic field Be^+ qubit

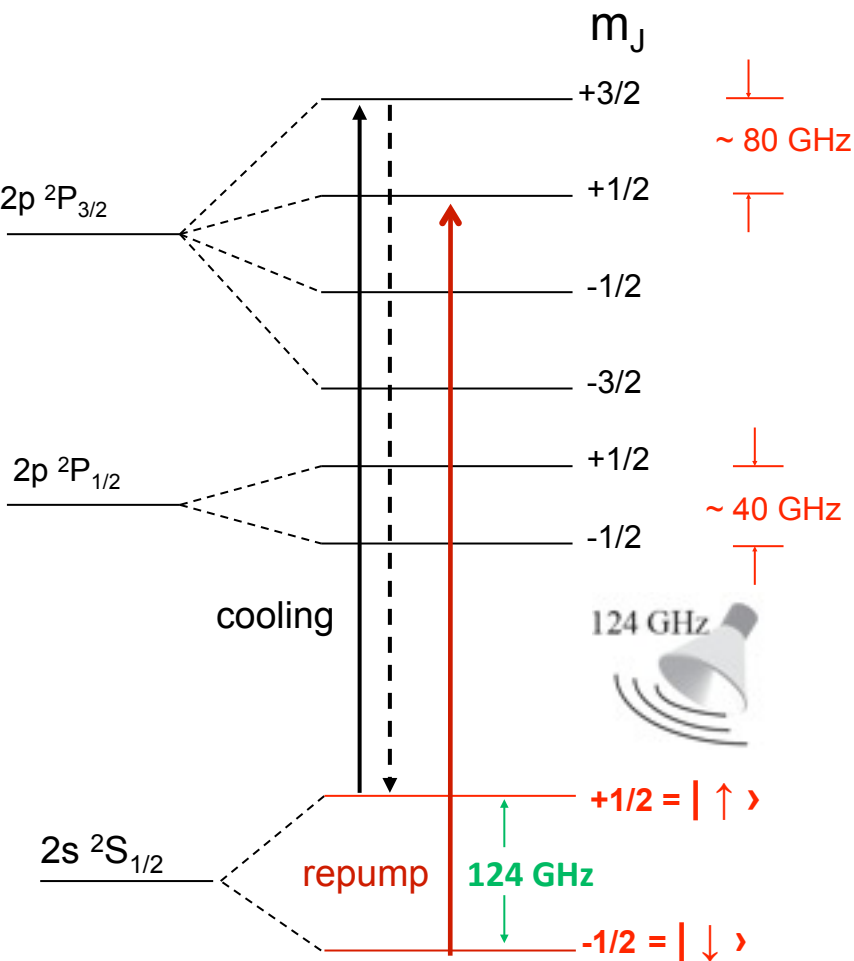
$^9\text{Be}^+$, $B \sim 4.6 \text{ T}$, $\omega_0 / 2\pi \sim 124.1 \text{ GHz}$

Rabi flopping with 150 mW, 124 GHz μW source

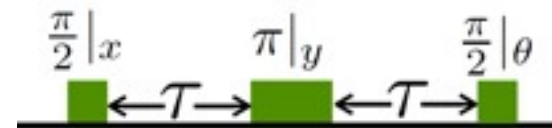


High magnetic field Be⁺ qubit

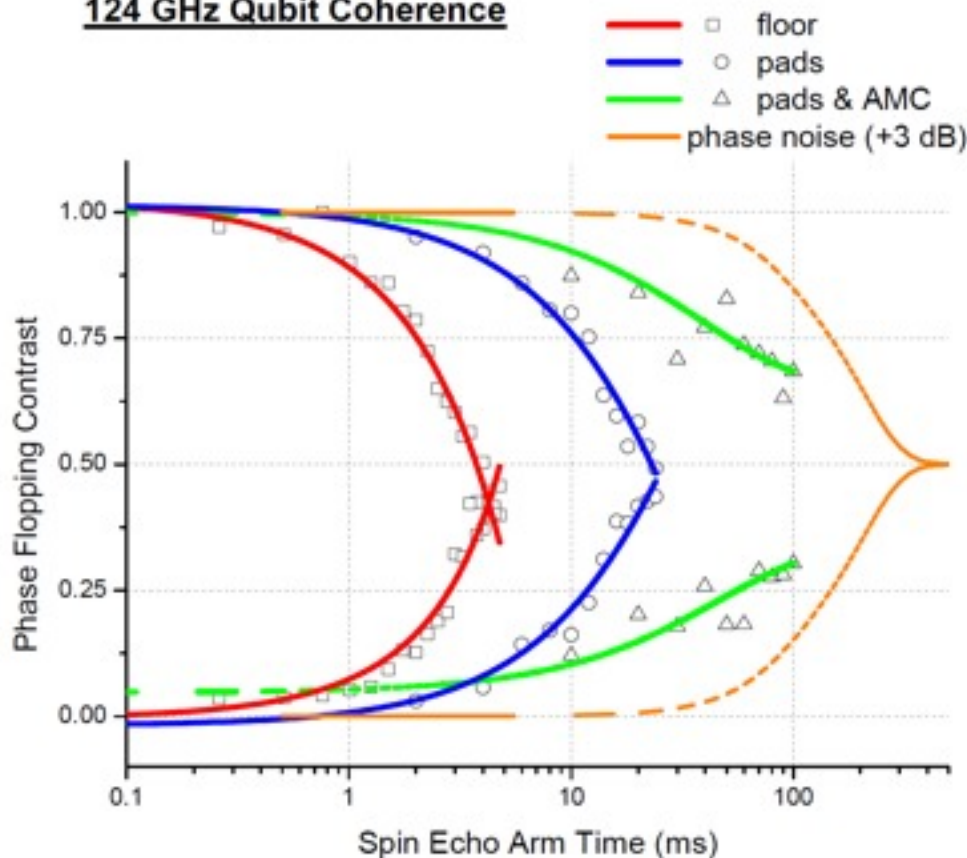
⁹Be⁺, B~4.6 T, $\omega_0/2\pi \sim 124.1$ GHz



Rabi flopping with 150 mW, 124 GHz μ W source

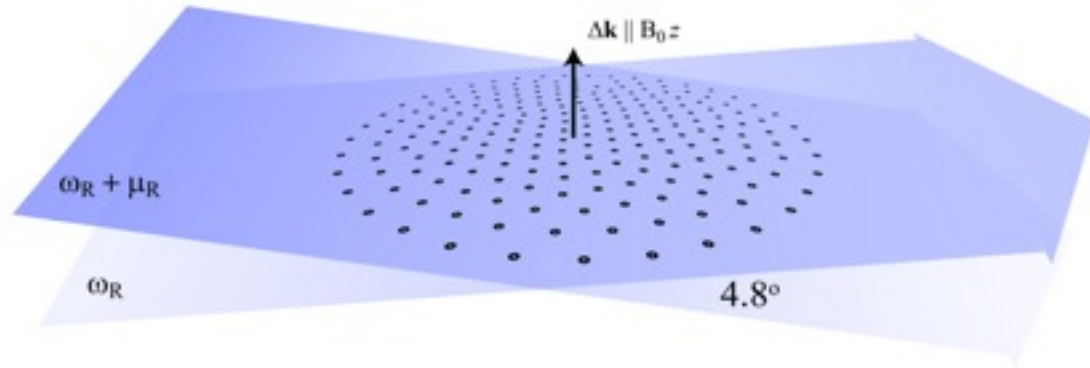
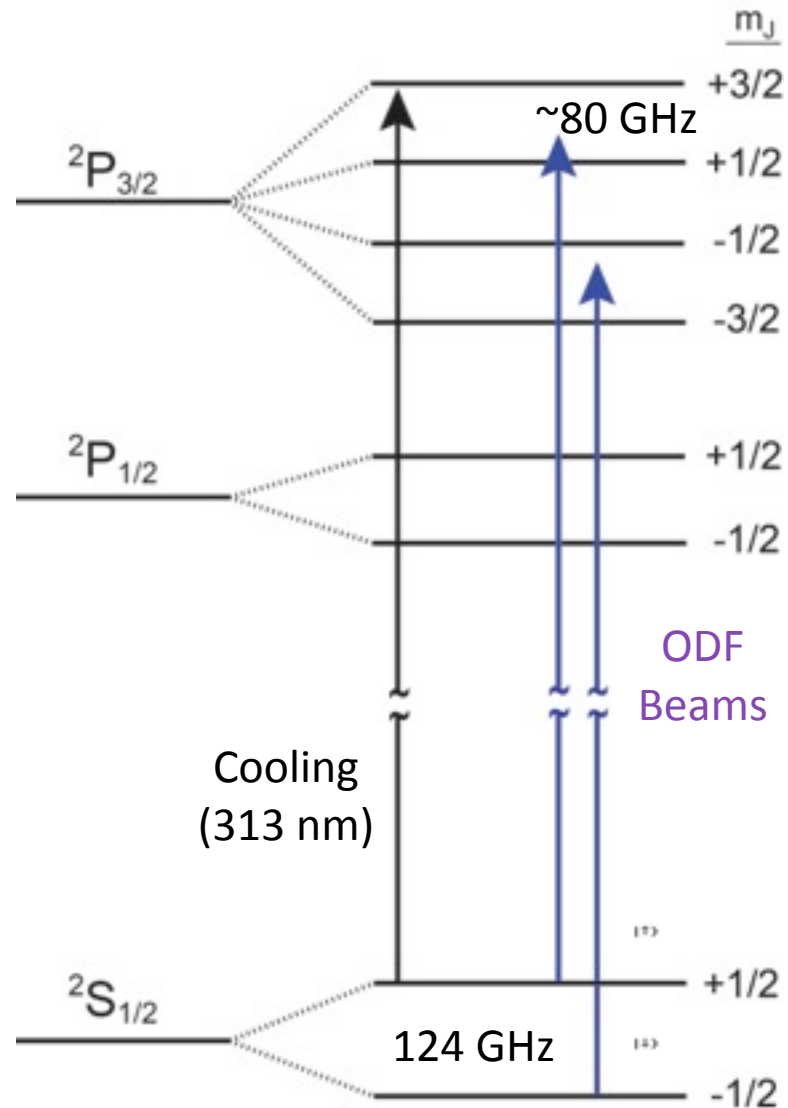


124 GHz Qubit Coherence



Engineer spin-spin interaction with spin-dependent optical dipole force

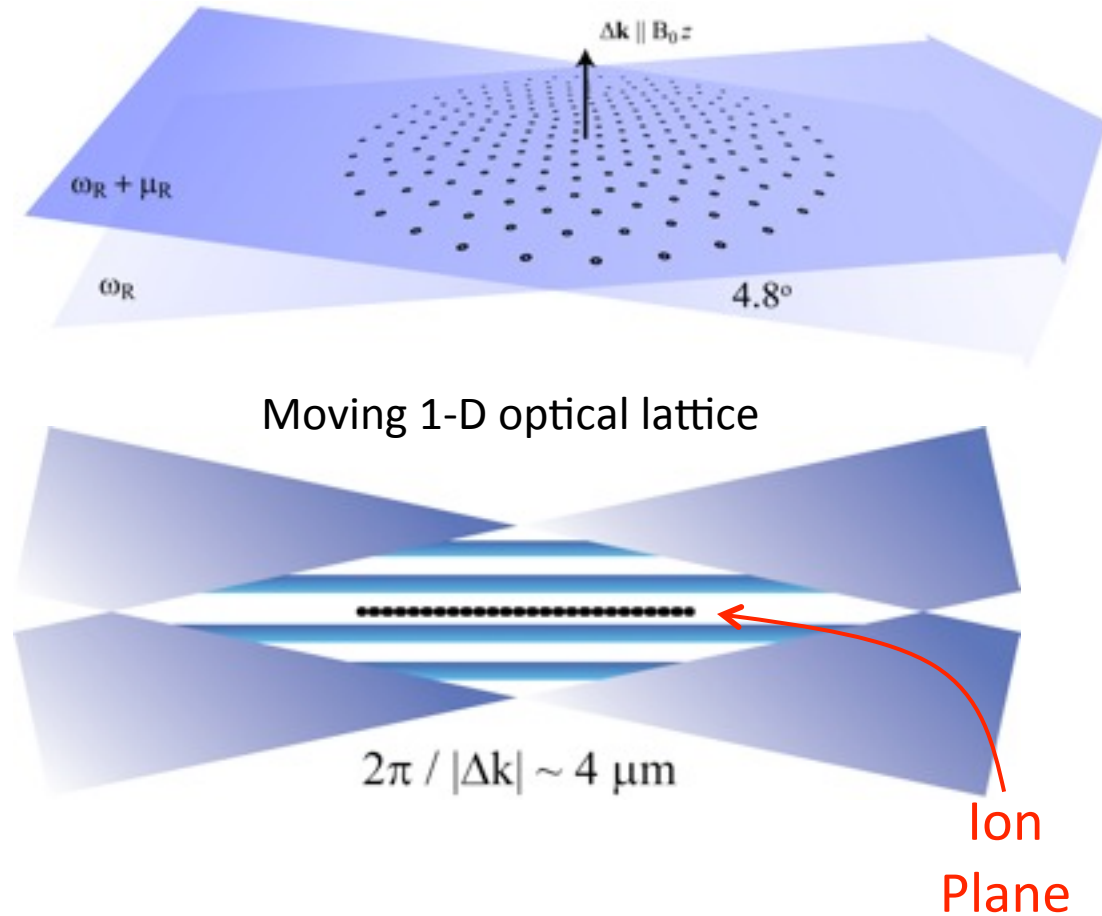
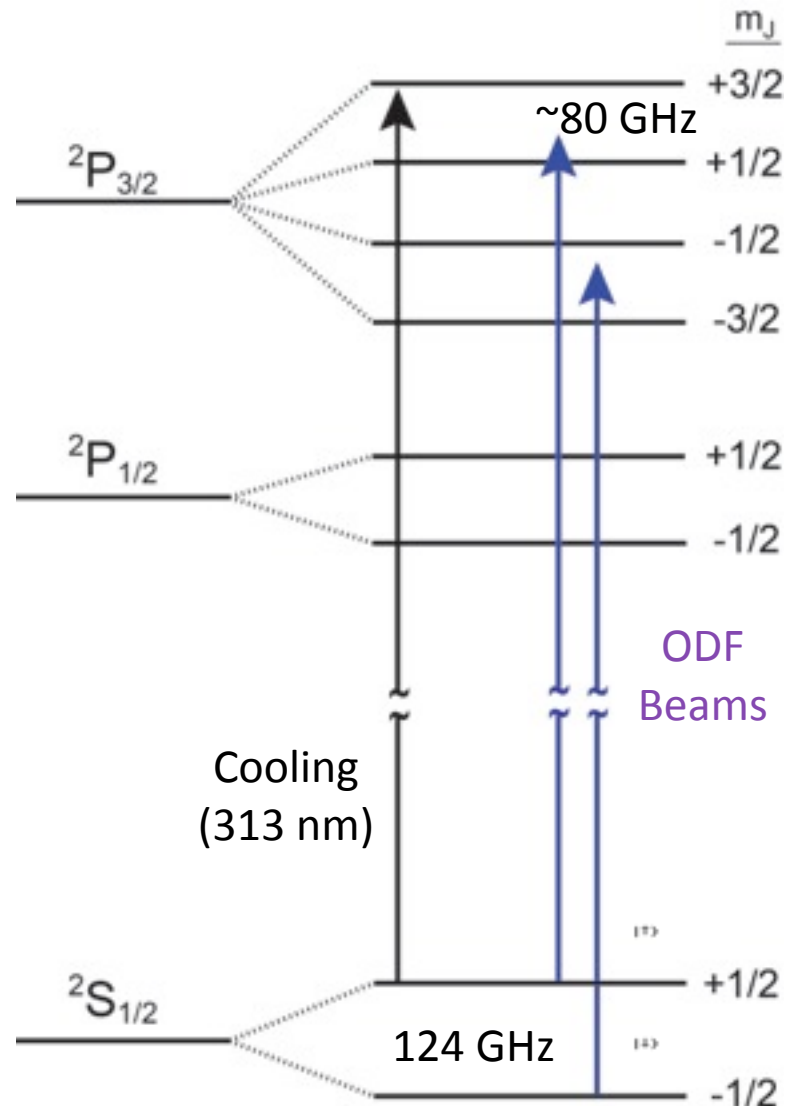
Leibfried et al., Nature **422**, 412-415 (2003)



beam waists $\sim 2000 \mu\text{m} \times 200 \mu\text{m}$
intensity $\sim 1 \text{ W/cm}^2$ per beam

Engineer spin-spin interaction with spin-dependent optical dipole force

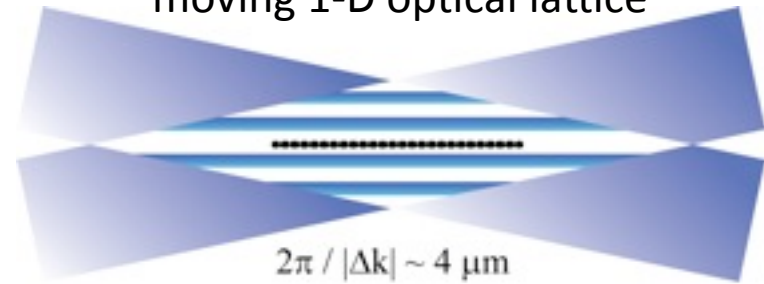
Leibfried et al., Nature **422**, 412-415 (2003)



● alignment of 1D lattice and ion plane crucial

Engineer spin-spin interaction with spin-dependent optical dipole force

moving 1-D optical lattice



$$2\pi / |\Delta k| \sim 4 \mu\text{m}$$

- $F_{\uparrow}(t) = -F_{\downarrow}(t)$
 $F_{\uparrow}(t) = F_0 \cos(\mu_R t)$

N transverse eigenmodes ω_m, \vec{b}_m ; eigenmodes calculated with code from Freericks group, Georgetown Univ.

$$\hat{H}_{ODF} = -F_0 \cos(\mu_R t) \sum_{j=1}^N \hat{z}_j \otimes \hat{\sigma}_j^z =$$

$$-F_0 \cos(\mu_R t) \sum_{j=1}^N \sum_{m=1}^N b_{jm} \sqrt{\frac{\hbar}{2M\omega_m}} \left(\hat{a}_m^\dagger e^{i\omega_m t} + \hat{a}_m e^{-i\omega_m t} \right) \hat{\sigma}_j^z$$

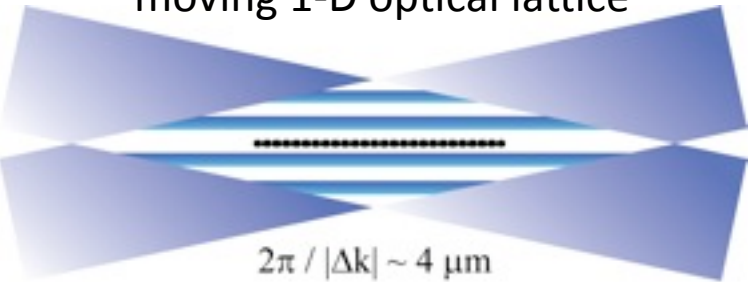
$$U(\tau) = \exp \left(\sum_i \hat{\phi}_i \hat{\sigma}_i^z + i \sum_{i,j} \phi_{ij} \hat{\sigma}_i^z \hat{\sigma}_j^z \right)$$

$$\hat{\phi}_i = \sum_m \alpha_{im}(\tau) \hat{a}_m^\dagger - \alpha_{im}^*(\tau) \hat{a}_{im}$$

$$\phi_{ij} \approx \frac{F_0^2}{2\hbar M} \sum_m \frac{b_{im} b_{jm}}{\mu_R^2 - \omega_m^2} \otimes$$

Engineer spin-spin interaction with spin-dependent optical dipole force

moving 1-D optical lattice



$$2\pi / |\Delta k| \sim 4 \mu\text{m}$$

$$\hat{H}_{ODF} = -F_0 \cos(\mu_R t) \sum_{j=1}^N \hat{z}_j \otimes \hat{\sigma}_j^z =$$

$$-F_0 \cos(\mu_R t) \sum_{j=1}^N \sum_{m=1}^N b_{jm} \sqrt{\frac{\hbar}{2M\omega_m}} (\hat{a}_m^\dagger e^{i\omega_m t} + \hat{a}_m e^{-i\omega_m t}) \hat{\sigma}_j^z$$

- $F_\uparrow(t) = -F_\downarrow(t)$
 $F_\uparrow(t) = F_0 \cos(\mu_R t)$

N transverse eigenmodes ω_m, \vec{b}_m ; eigenmodes calculated with code from Freericks group, Georgetown Univ.

$$U(\tau) = \exp\left(\sum_i \hat{\phi}_i \hat{\sigma}_i^z + i \sum_{i,j} \phi_{ij} \hat{\sigma}_i^z \hat{\sigma}_j^z \right)$$

Displacement

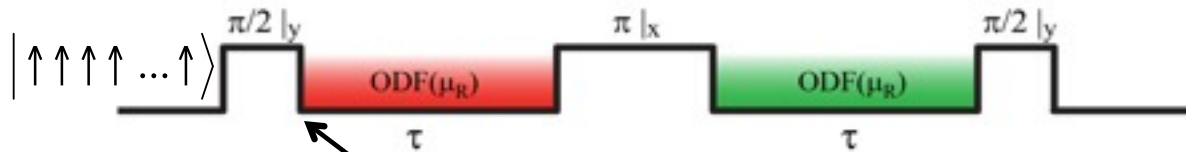
$$\hat{\phi}_i = \sum_m \alpha_{im}(\tau) \hat{a}_m^\dagger - \alpha_{im}^*(\tau) \hat{a}_{im}$$

spin-motion entanglement →
decoherence in spin Bloch vector

spin-spin coupling

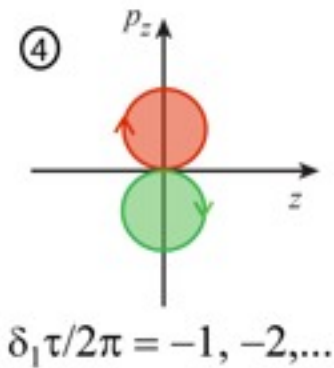
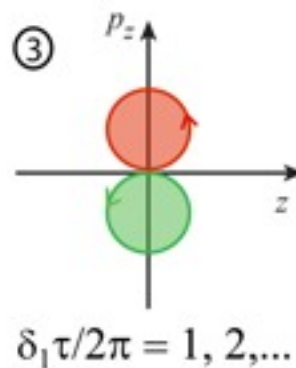
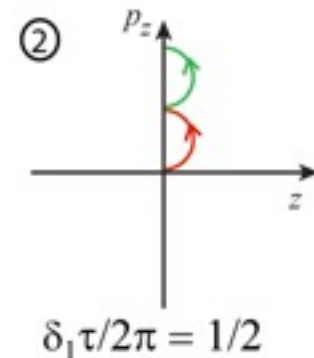
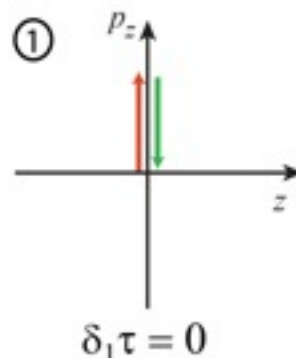
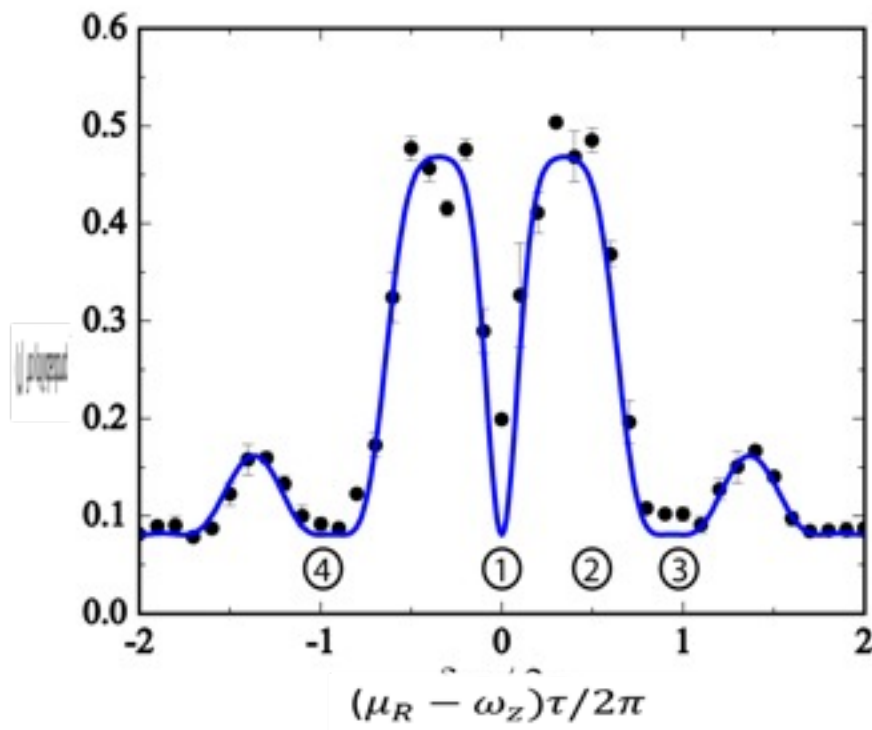
$$\phi_{ij} \approx \frac{F_0^2}{2\hbar M} \sum_m \frac{b_{im} b_{jm}}{\mu_R^2 - \omega_m^2} \otimes$$

Spin-motion entanglement \rightarrow spectroscopy and thermometry of transverse modes

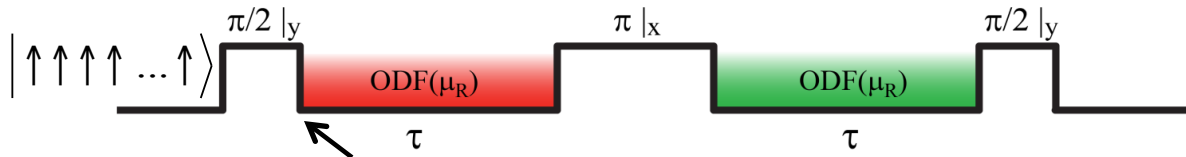


$$\prod_i \left(\frac{|\uparrow\rangle_i + |\downarrow\rangle_i}{\sqrt{2}} \right)$$

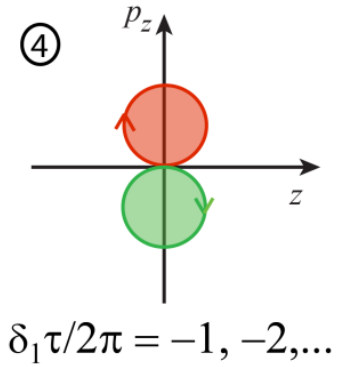
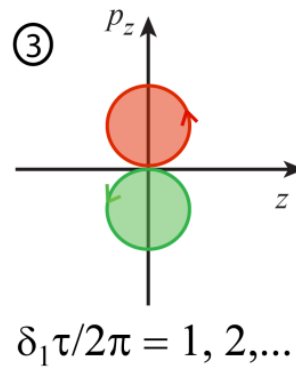
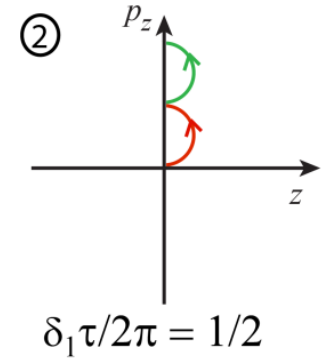
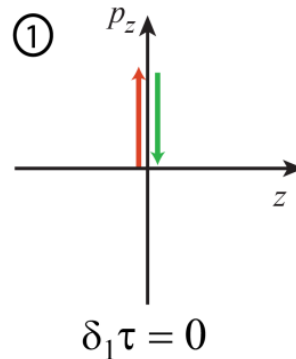
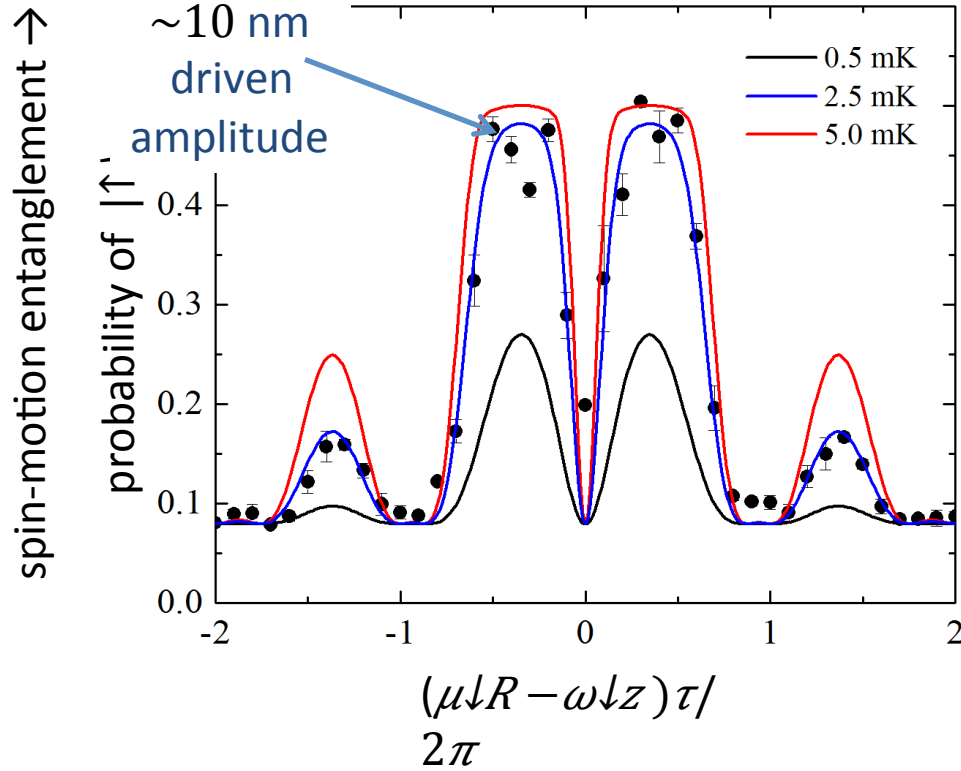
spin-motion entanglement \rightarrow



Spin-motion entanglement \rightarrow spectroscopy and thermometry of transverse modes

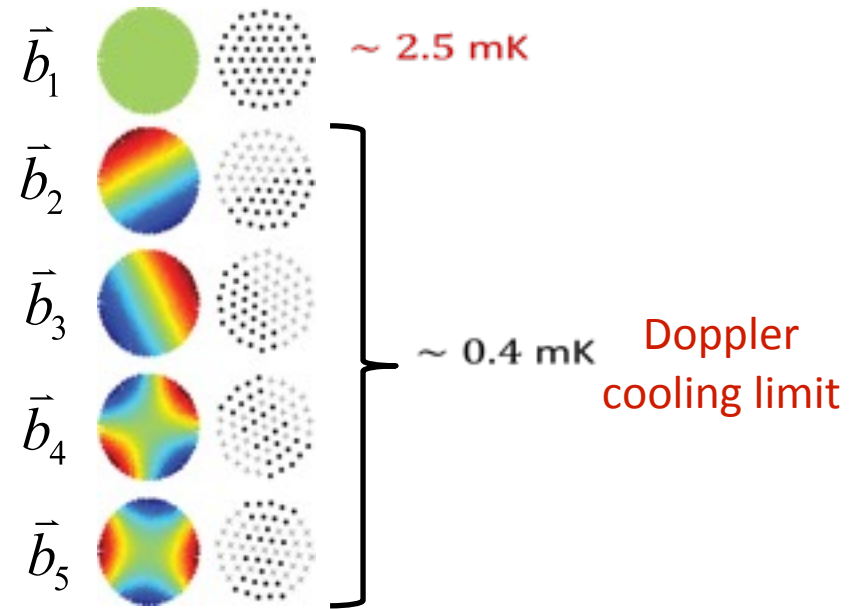
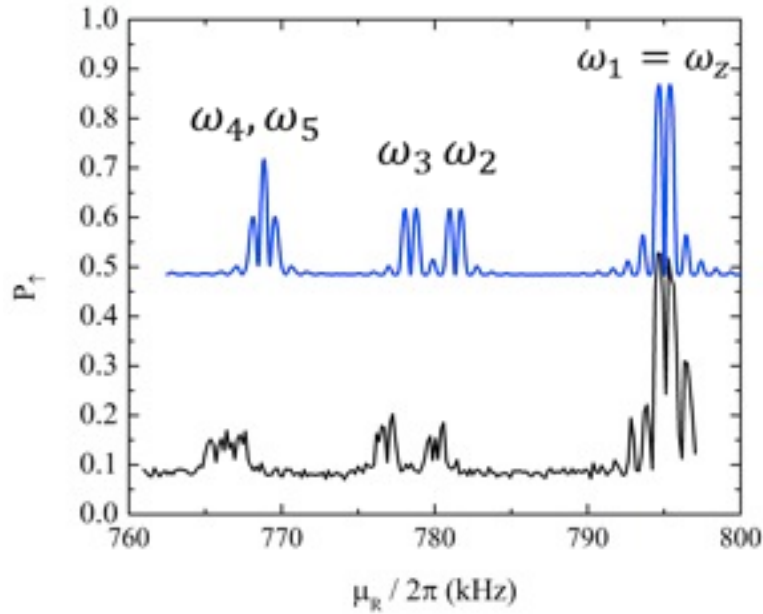


$$\prod_i \left(\frac{|\uparrow\rangle_i + |\downarrow\rangle_i}{\sqrt{2}} \right)$$

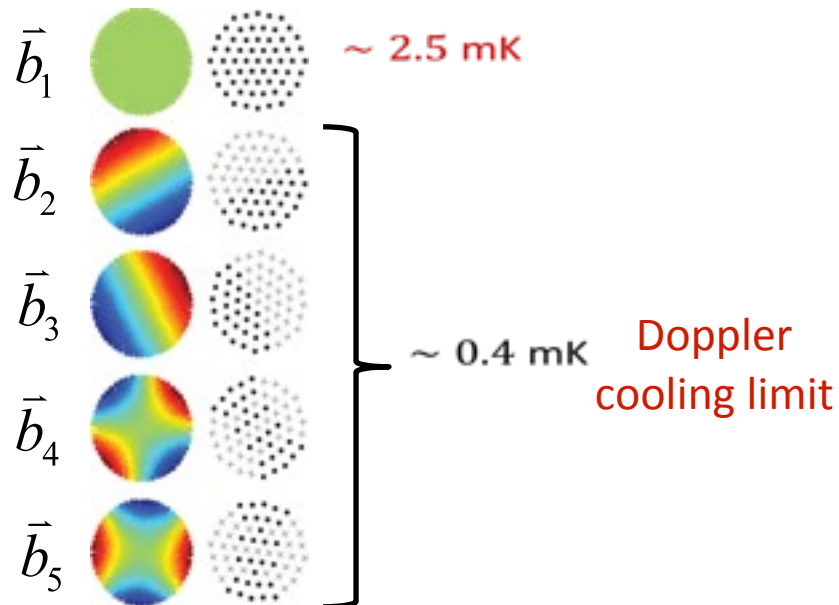
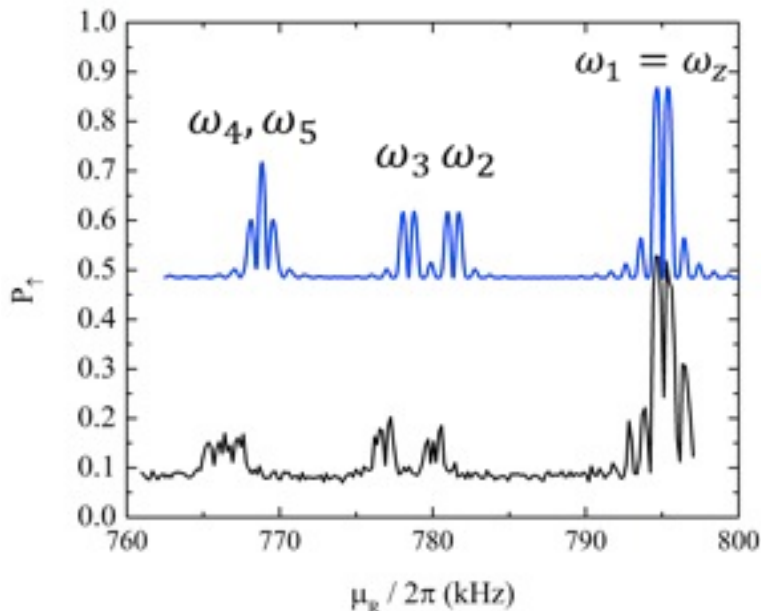


$$P_{\uparrow} = \frac{1}{2} \left(1 - e^{-2|\alpha|^2(2\bar{n}+1)} \right) \quad \alpha(t) = \langle z(t) + ip_z(t) \rangle \text{ is the coherently driven amplitude}$$

Spin-motion entanglement \rightarrow spectroscopy and thermometry of transverse modes

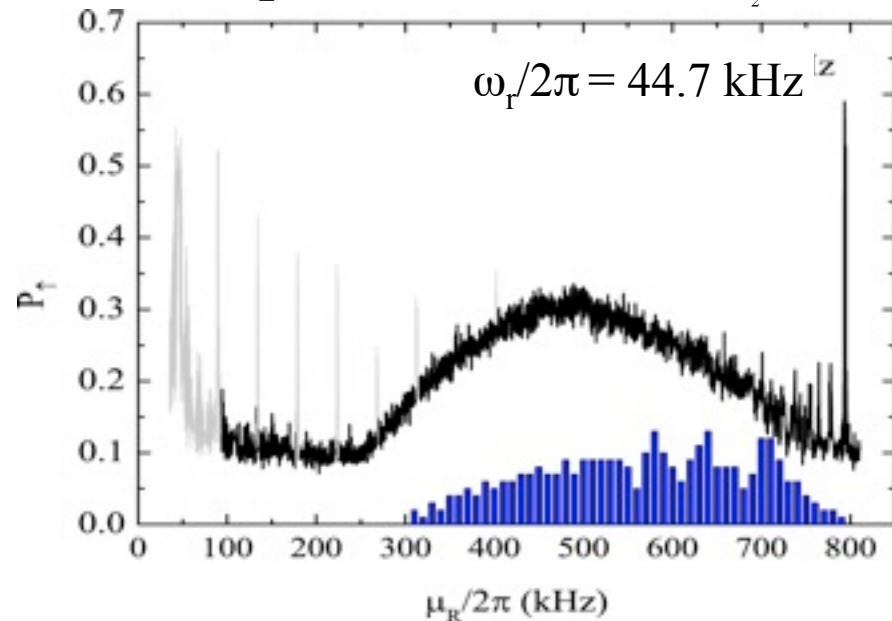
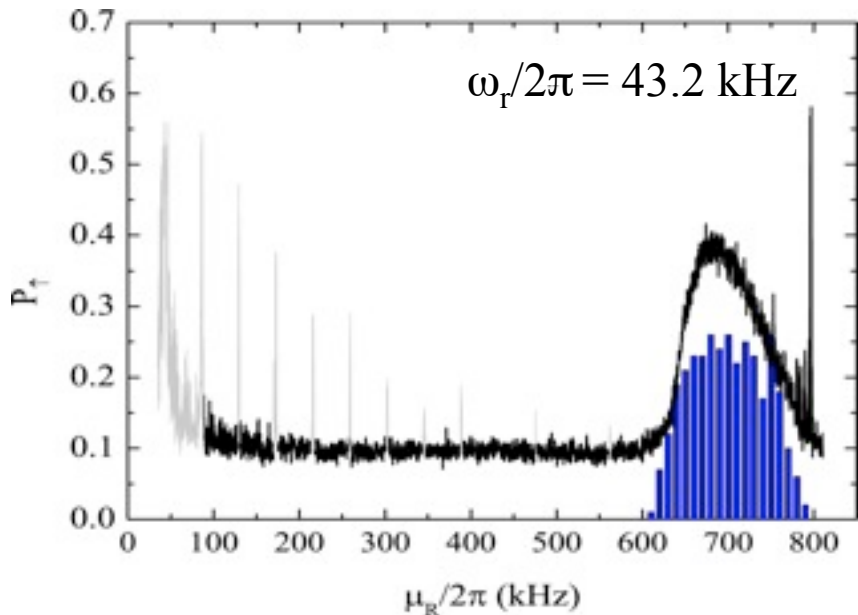


Spin-motion entanglement \rightarrow spectroscopy and thermometry of transverse modes



Broad sweep over all ($N > 300$) transverse modes

$$q\Phi_{trap}(r, z) = \frac{1}{2} m\omega_z^2 (z^2 + \beta(\omega_r)r^2) \quad \beta \equiv \frac{\omega_r(\Omega_c - \omega_r)}{\omega_z^2} - \frac{1}{2}$$



spin-spin coupling with spin-dependent optical dipole force

$$H_{\text{Ising}} = \frac{1}{N} \sum_{i < j} J_{i,j} \sigma_i^z \sigma_j^z, J_{i,j} = \frac{F_0^2 N}{\hbar \times 2M} \sum_{m=1}^N \frac{b_{i,m} b_{j,m}}{\mu_R^2 - \omega_m^2}$$

Theory – Freericks Georgetown group



ω_1

ω_{COM}



ω_2

ω_{tilt}



ω_3

ω_{tilt}



ω_4

ω_{chip}



ω_5

ω_{chip}



ω_6



ω_7



ω_8



ω_9

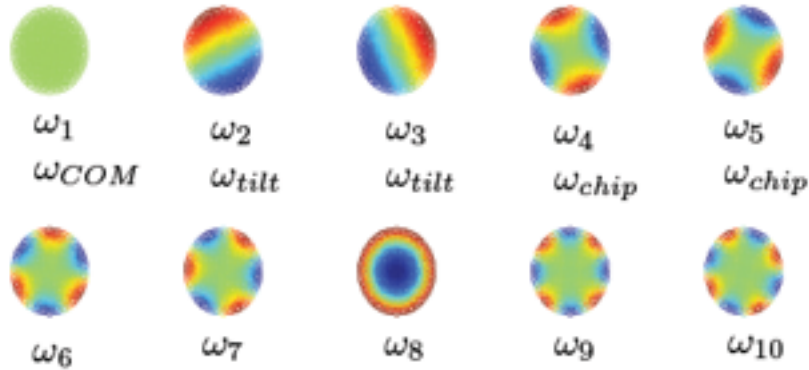


ω_{10}

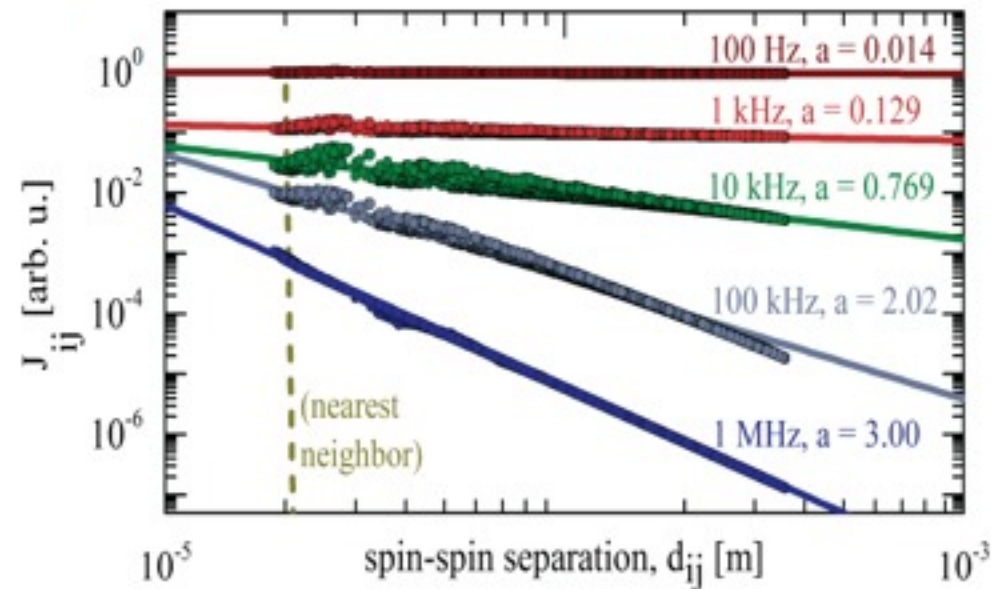
spin-spin coupling with spin-dependent optical dipole force

$$H_{\text{Ising}} = \frac{1}{N} \sum_{i < j} J_{i,j} \sigma_i^z \sigma_j^z, J_{i,j} = \frac{F_0^2 N}{\hbar \times 2M} \sum_{m=1}^N \frac{b_{i,m} b_{j,m}}{\mu_R^2 - \omega_m^2}$$

Theory – Freericks Georgetown group



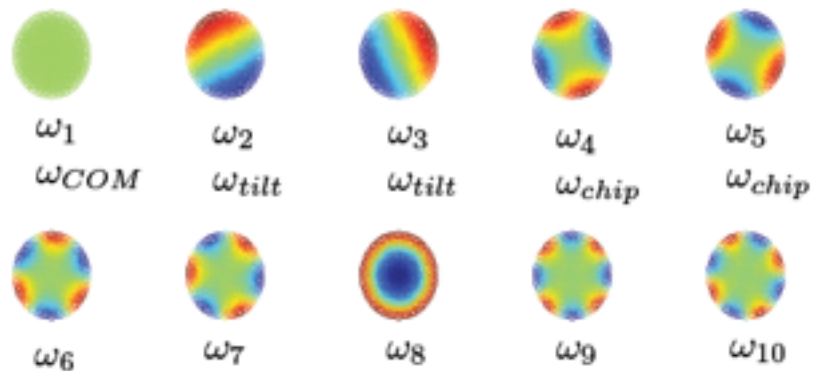
power-law interaction range $J_{i,j} \propto d_{i,j}^{-a}$



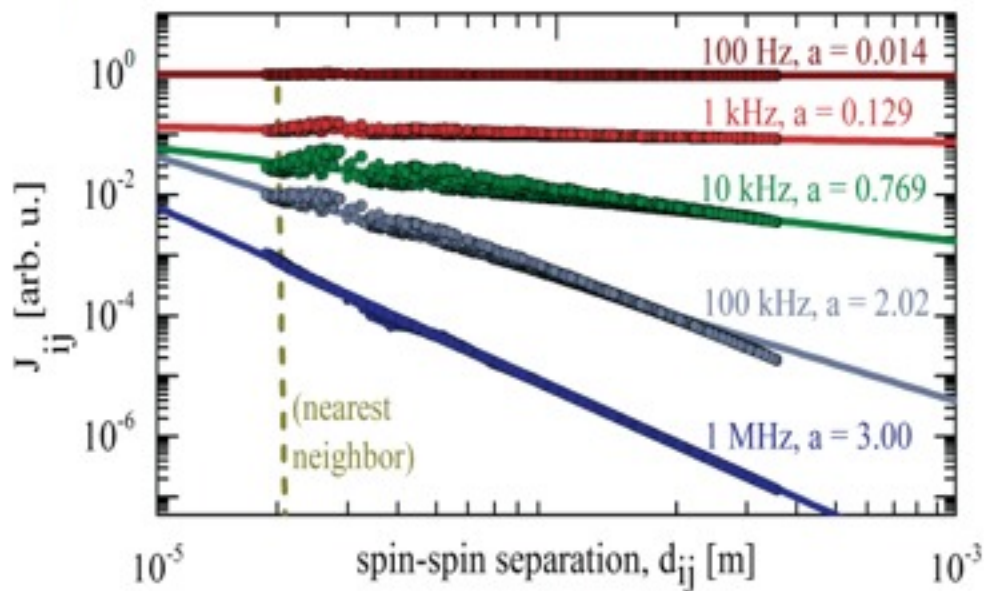
spin-spin coupling with spin-dependent optical dipole force

$$H_{\text{Ising}} = \frac{1}{N} \sum_{i < j} J_{i,j} \sigma_i^z \sigma_j^z, J_{i,j} = \frac{F_0^2 N}{\hbar \times 2M} \sum_{m=1}^N \frac{b_{i,m} b_{j,m}}{\mu_R^2 - \omega_m^2}$$

Theory – Freericks Georgetown group



power-law interaction range $J_{i,j} \propto d_{i,j}^{-a}$

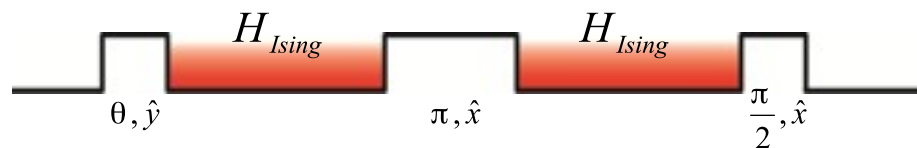
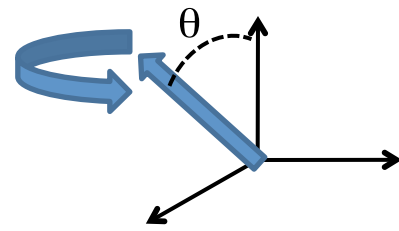


Benchmarking for $\omega_z < \mu_R < \omega_z + (2\pi)35$ kHz

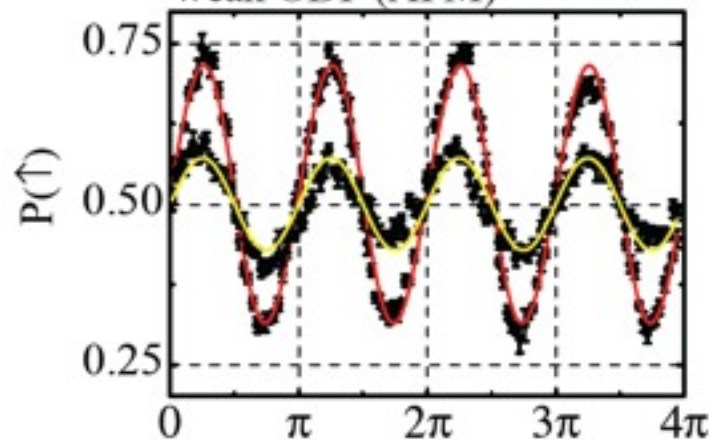
- measure mean-field spin precession

$$\omega_{\text{precession}} \sim \bar{J} \times \cos(\theta)$$

$$\bar{J} = \frac{1}{N^2} \sum_{i \neq j} J_{i,j}$$



weak ODF (AFM)



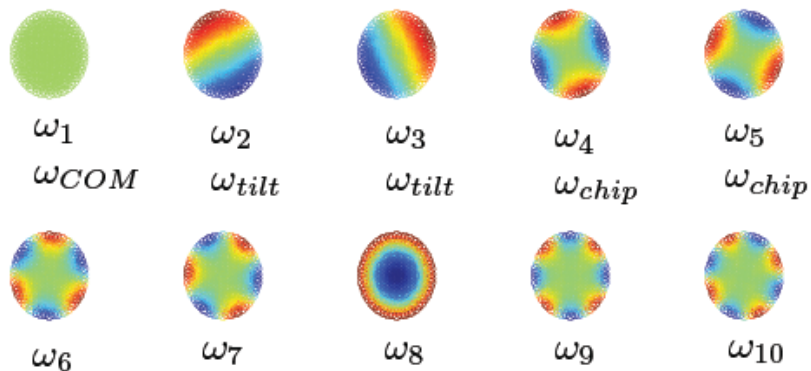
$$P(\uparrow) = \frac{1}{2} \left[1 + e^{-\Gamma \times 2\tau_{\text{arm}}} \sin(\theta) \sin(2\bar{J} \cos(\theta) \times 2\tau_{\text{arm}}) \right]$$

single parameter fit $\rightarrow \bar{J}$

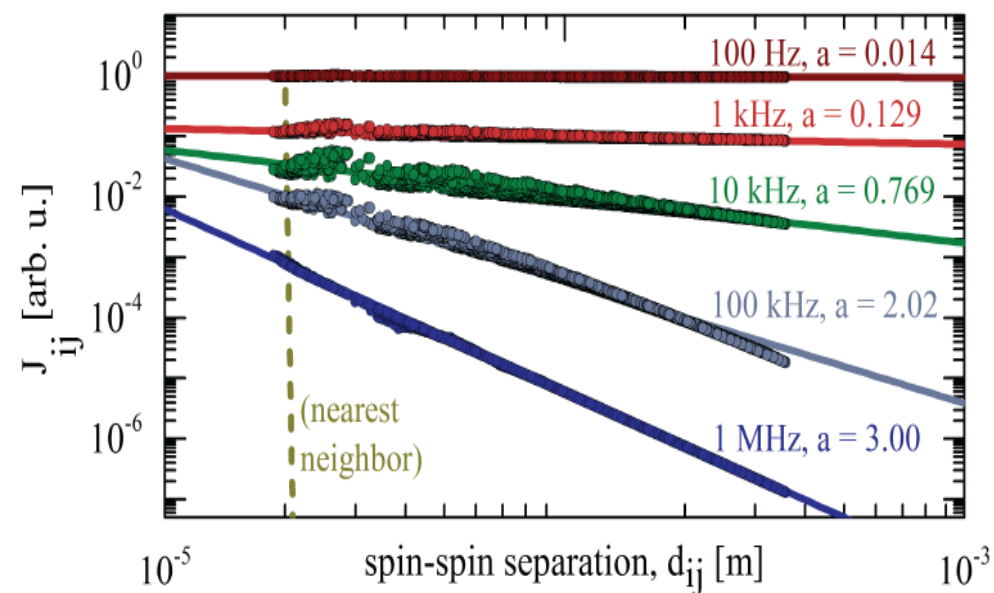
spin-spin coupling with spin-dependent optical dipole force

$$H_{\text{Ising}} = \frac{1}{N} \sum_{i < j} J_{i,j} \sigma_i^z \sigma_j^z, J_{i,j} = \frac{F_0^2 N}{\hbar \cdot 2M} \sum_{m=1}^N \frac{b_{i,m} b_{j,m}}{\mu_R^2 - \omega_m^2}$$

Theory – Freericks Georgetown group



power-law interaction range $J_{i,j} \propto d_{i,j}^{-a}$

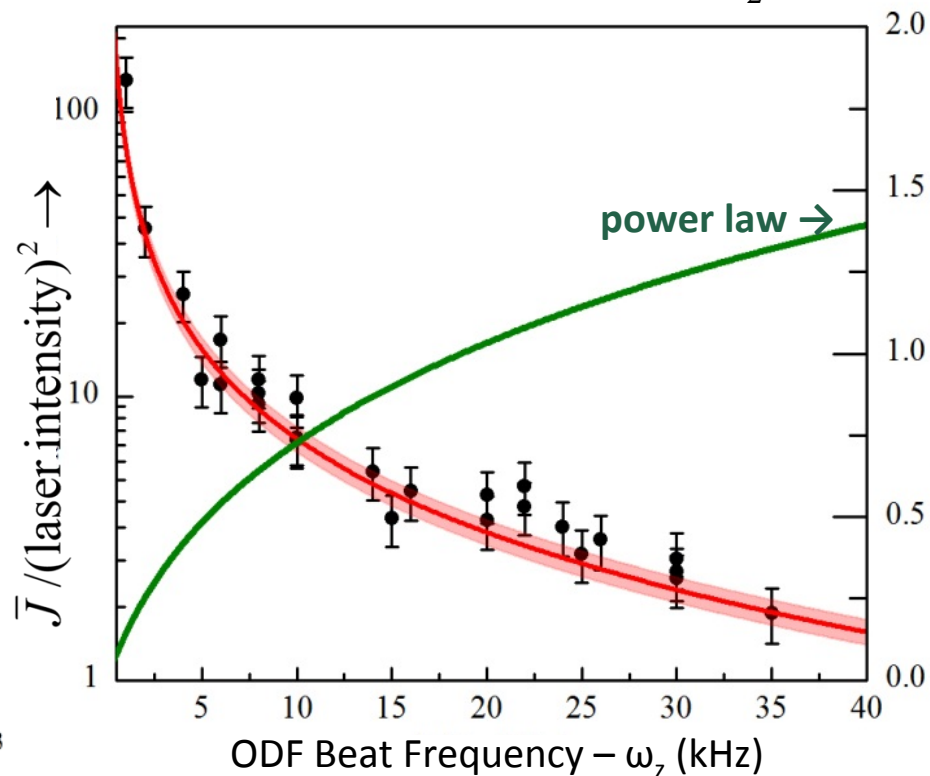
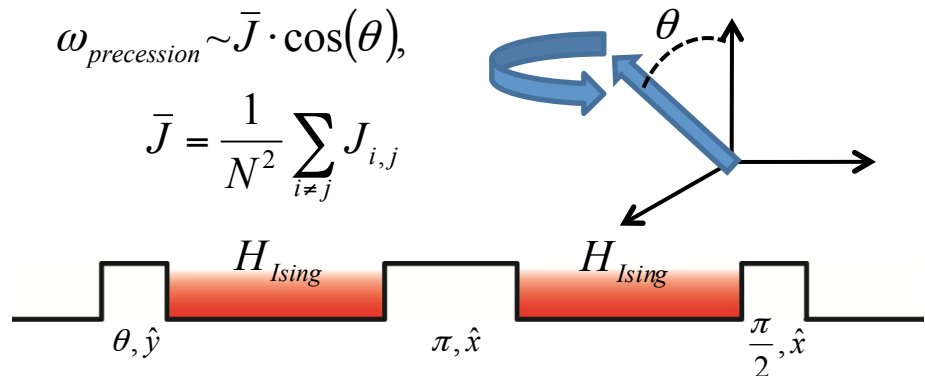


Benchmarking for $\omega_z < \mu_R < \omega_z + (2\pi)35$ kHz

- measure mean-field spin precession

$$\omega_{\text{precession}} \sim \bar{J} \cdot \cos(\theta),$$

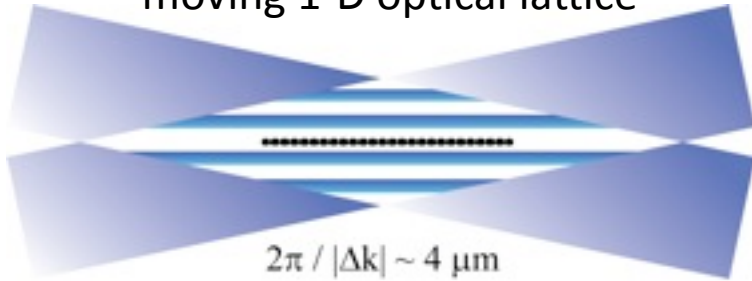
$$\bar{J} = \frac{1}{N^2} \sum_{i \neq j} J_{i,j}$$



Multi-qubit control - Entanglement and control with many ions in Penning traps

Britton, Sawyer, Bollinger

- mean field analysis and spin precession measurement benchmark Ising interaction strength moving 1-D optical lattice

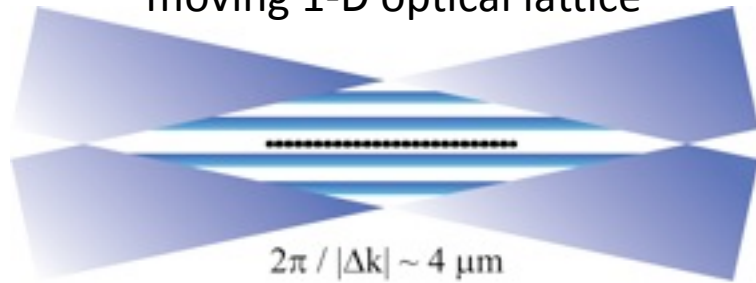


$$H_{\text{Ising}} = \frac{1}{N} \sum_{i < j} J_{i,j} \sigma_i^z \sigma_j^z, J_{i,j} = \frac{F_0^2 N}{\hbar \times 2M} \sum_{m=1}^N \frac{b_{i,m} b_{j,m}}{\mu_R^2 - \omega_m^2}$$

Multi-qubit control - Entanglement and control with many ions in Penning traps

Britton, Sawyer, Bollinger

- mean field analysis and spin precession measurement benchmark Ising interaction strength moving 1-D optical lattice



$$H_{\text{Ising}} = \frac{1}{N} \sum_{i < j} J_{i,j} \sigma_i^z \sigma_j^z, J_{i,j} = \frac{F_0^2 N}{\hbar \times 2M} \sum_{m=1}^N \frac{b_{i,m} b_{j,m}}{\mu_R^2 - \omega_m^2}$$

- H_{Ising} should generate entanglement

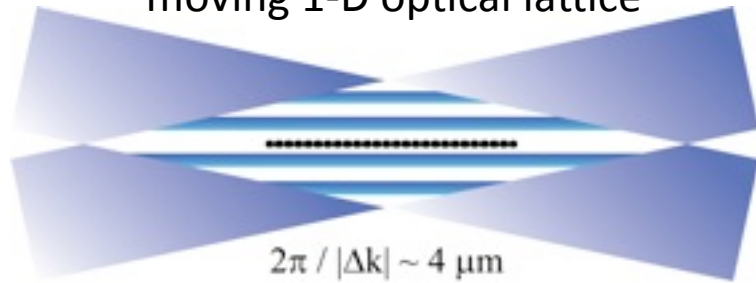
$$\text{For } \mu_R \approx \omega_z, J_{i,j} \approx \frac{F_0^2}{\hbar \times 2M} \times \frac{1}{\mu_R^2 - \omega_m^2} \equiv \chi$$

$$H_{\text{Ising}} \approx \frac{2\chi}{N} \times J_z^2, J_z = \sum_i \sigma_i^z / 2 \quad \text{spin squeezing}$$

Multi-qubit control - Entanglement and control with many ions in Penning traps

Britton, Sawyer, Bollinger

- mean field analysis and spin precession measurement benchmark Ising interaction strength moving 1-D optical lattice



$$H_{\text{Ising}} = \frac{1}{N} \sum_{i < j} J_{i,j} \sigma_i^z \sigma_j^z, J_{i,j} = \frac{F_0^2 N}{\hbar \times 2M} \sum_{m=1}^N \frac{b_{i,m} b_{j,m}}{\mu_R^2 - \omega_m^2}$$

- H_{Ising} should generate entanglement

$$\text{For } \mu_R \approx \omega_z, J_{i,j} \approx \frac{F_0^2}{\hbar \times 2M} \times \frac{1}{\mu_R^2 - \omega_m^2} \equiv \chi$$

$$H_{\text{Ising}} \approx \frac{2\chi}{N} \times J_z^2, J_z = \sum_i \sigma_i^z / 2$$

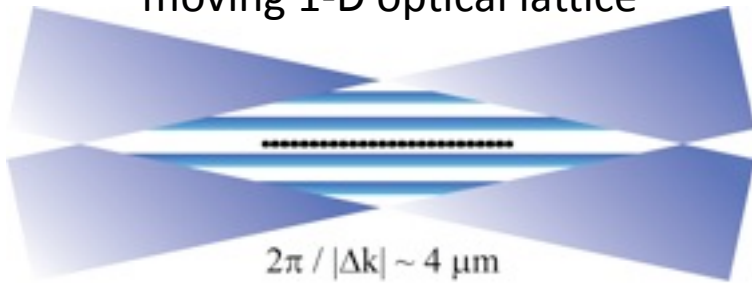
~~spin squeezing~~

not yet
observed

Multi-qubit control - Entanglement and control with many ions in Penning traps

Britton, Sawyer, Bollinger

- mean field analysis and spin precession measurement benchmark Ising interaction strength moving 1-D optical lattice



$$H_{\text{Ising}} = \frac{1}{N} \sum_{i < j} J_{i,j} \sigma_i^z \sigma_j^z, J_{i,j} = \frac{F_0^2 N}{\hbar \times 2M} \sum_{m=1}^N \frac{b_{i,m} b_{j,m}}{\mu_R^2 - \omega_m^2}$$

- H_{Ising} should generate entanglement

$$\text{For } \mu_R \approx \omega_z, J_{i,j} \approx \frac{F_0^2}{\hbar \times 2M} \times \frac{1}{\mu_R^2 - \omega_m^2} \equiv \chi$$

$$H_{\text{Ising}} \approx \frac{2\chi}{N} \times J_z^2, J_z = \sum_i \sigma_i^z / 2$$

~~spin squeezing~~

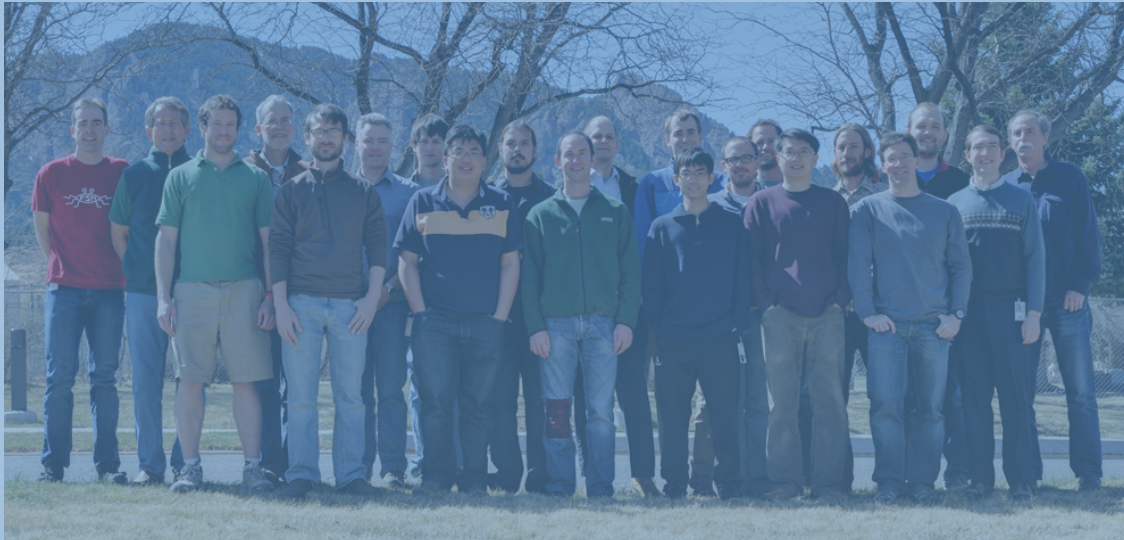
not yet observed

- planned improvements:

- individual spin detection in the rotating frame \rightarrow direct measurement of $\langle \sigma_i^z \sigma_j^z \rangle$

- increase angle between ODF beams (+/- 20°) \rightarrow minimize decoherence due to spontaneous emission

Trapped-ion metrology experiments at NIST



Ion Storage
Group
March 23, 2011

Jim Bergquist
Brad Blakestad (now JQI)
John Bollinger
Ryan Bowler
Joe Britton
Kenton Brown
James Chou
Yves Colombe
John Gaebler
David Hanneke (now at Amherst)
Dustin Hite
David Hume (now OFM)
Wayne Itano
Robert Jördens
John Jost
Dietrich Leibfried
Yiheng Lin
Christian Ospelkaus (now U Hannover)
Till Rosenband
Brian Sawyer
Ting-Rei Tan
Mike Thorpe
Ulrich Warring
Andrew Wilson
David Wineland

Quantum Measurement (Ancilla-assisted readout):

- Readout of the Al^+ clock state

Multi-qubit control:

- Entanglement and control with many ions in Penning traps

Entangled States:

- Generation of entangled states with microwave field gradients (novel schemes)
- Coupled ion trap spectroscopy (novel systems and applications)

Theme – Shared ion motion due to strong Coulomb interaction used to generate entanglement and read out quantum states



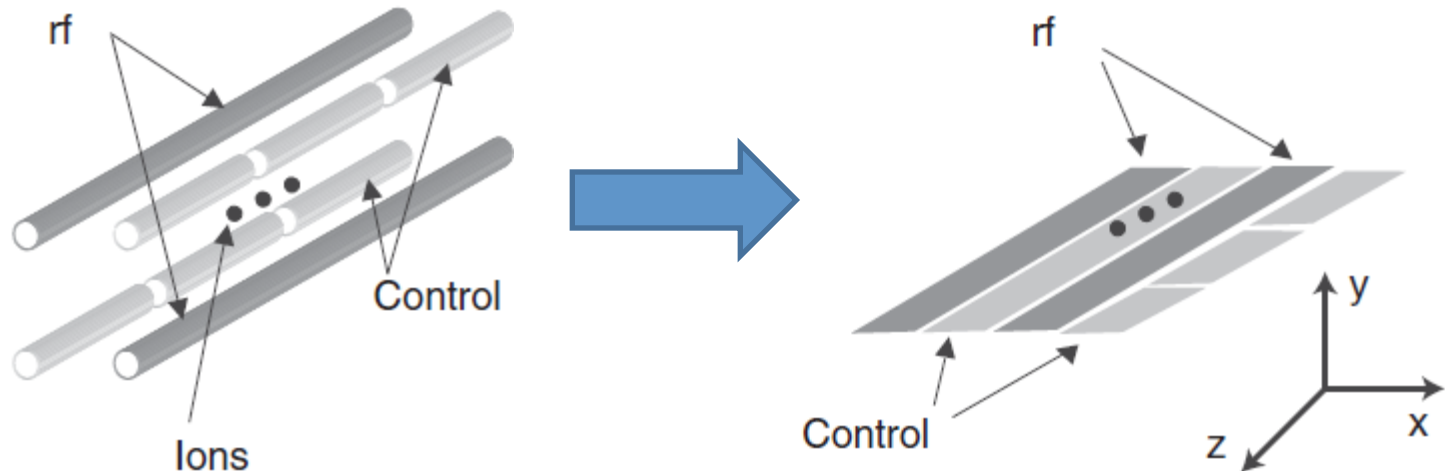
Generation of entangled states with microwave field gradients

Ospelkaus, Warring, Colombe, Brown, Amini, Leibfried, Wineland, Nature 476, 181 (2011)

Potential benefits of microwave gradients vs laser intensity gradients:

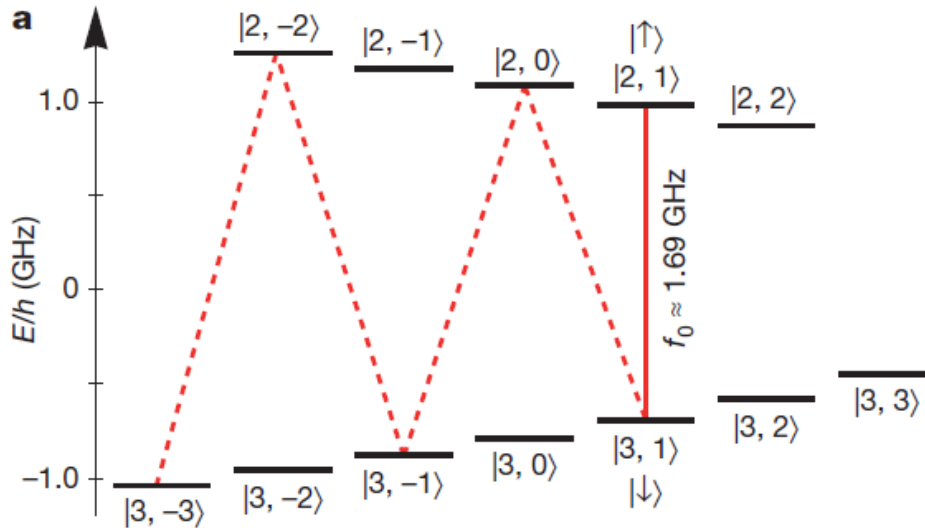
- better control with RF/microwaves
- no spontaneous emission
- ground state cooling not necessary (small Lamb-Dicke parameter)
- laser overhead vastly reduced

Requirement of strong microwave field gradient \rightarrow use near field from microwave currents in surface electrode ion traps

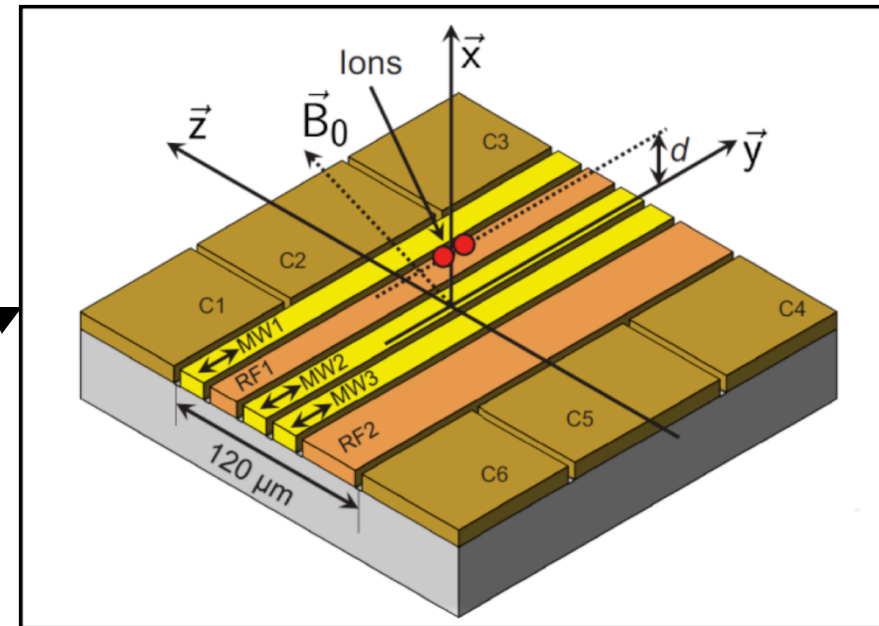
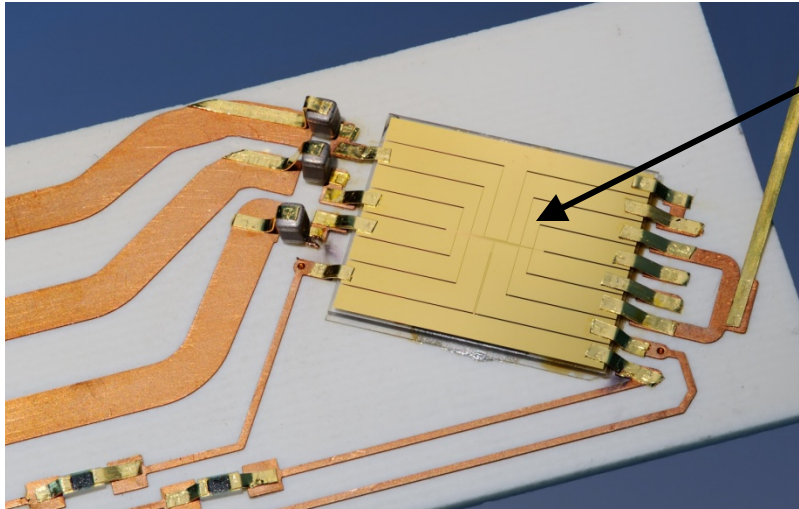


Generation of entangled states with microwave field gradients

Ospelkaus, Warring, Colombe, Brown, Amini, Leibfried, Wineland, Nature 476, 181 (2011)



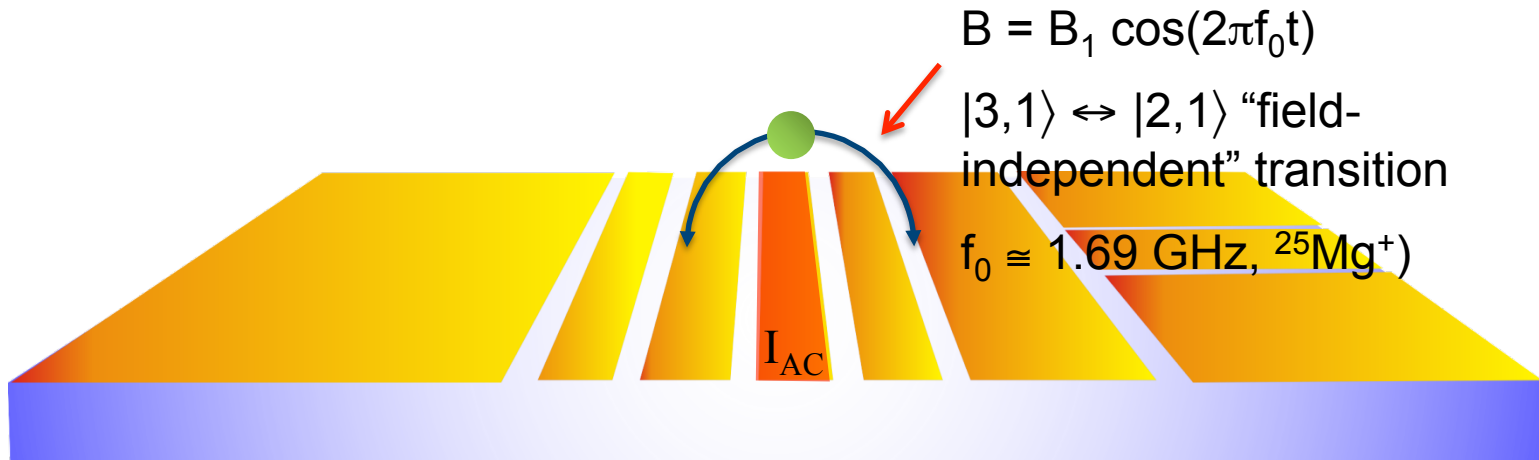
$^{25}\text{Mg}^+$, radial trap frequency ≈ 5 MHz,
 $B_0 = 21.3$ mT
ion – electrode distance = $30 \mu\text{m}$
 $dB_{\text{uW}}/dz \approx 35$ T/m



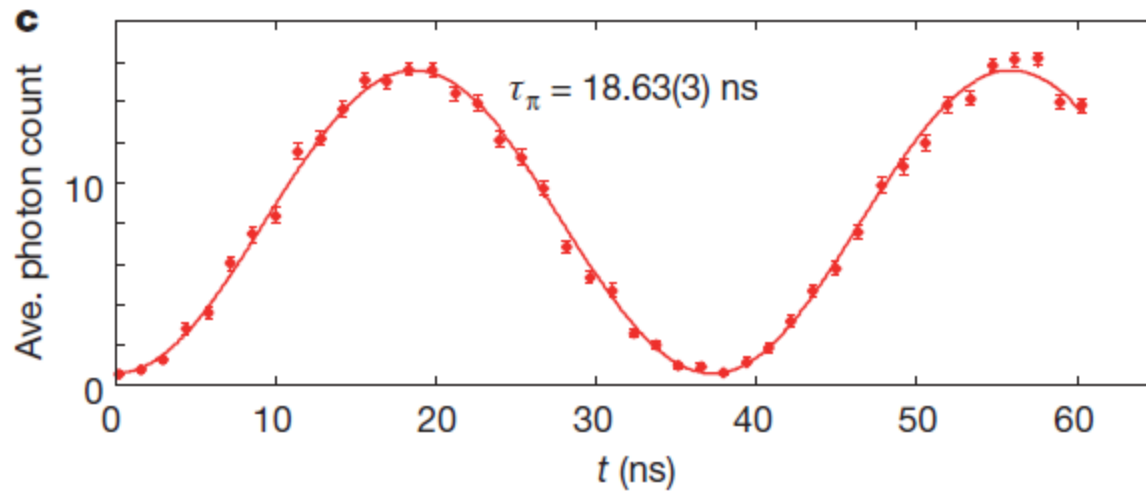
C. Ospelkaus *et al.*, PRL **101**, 090502 (2008)

C. Ospelkaus *et al.*, Nature, **476**, 181 (2011)

Single-qubit gates (Rabi flopping)

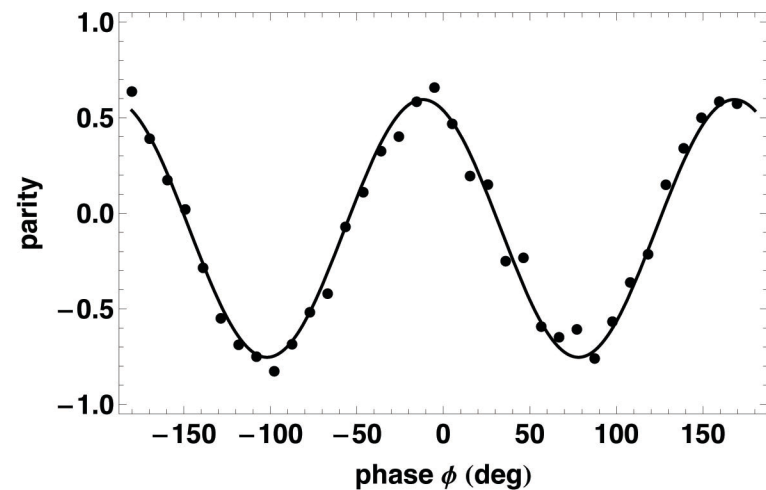
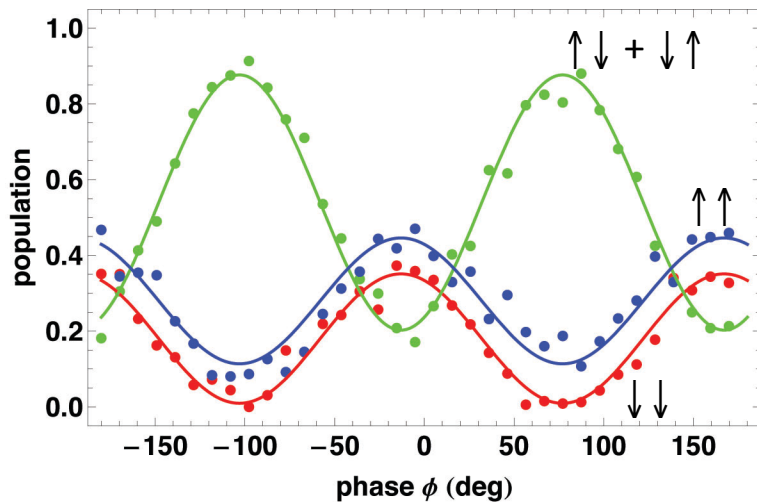
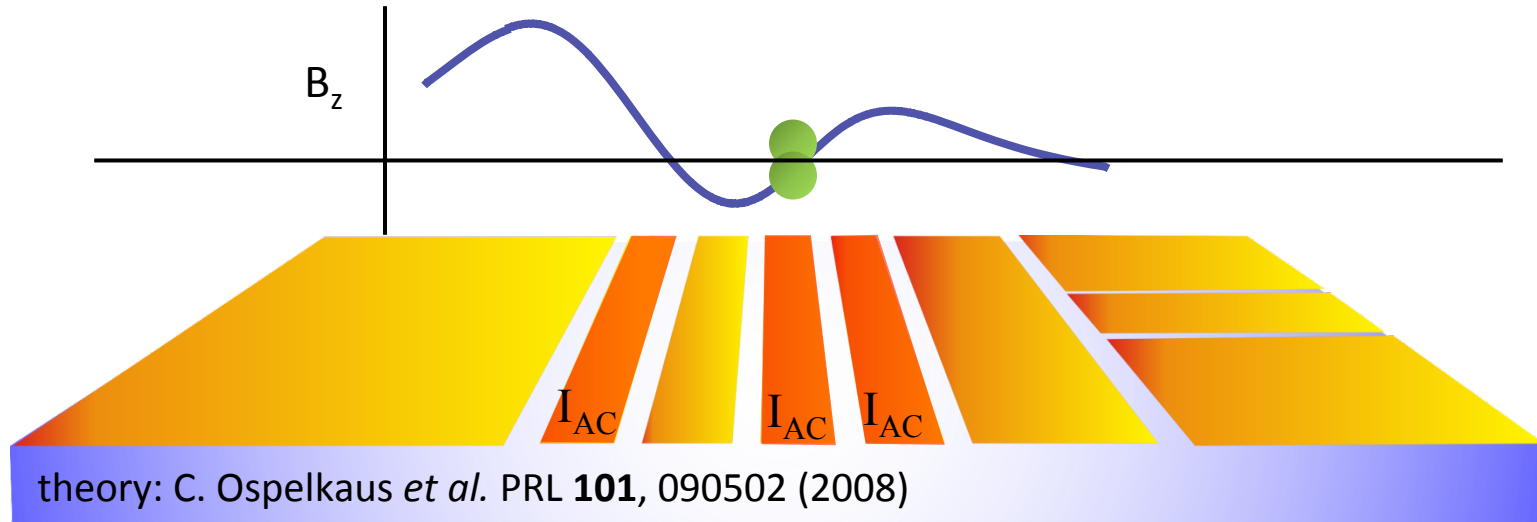


**Rabi
flopping**



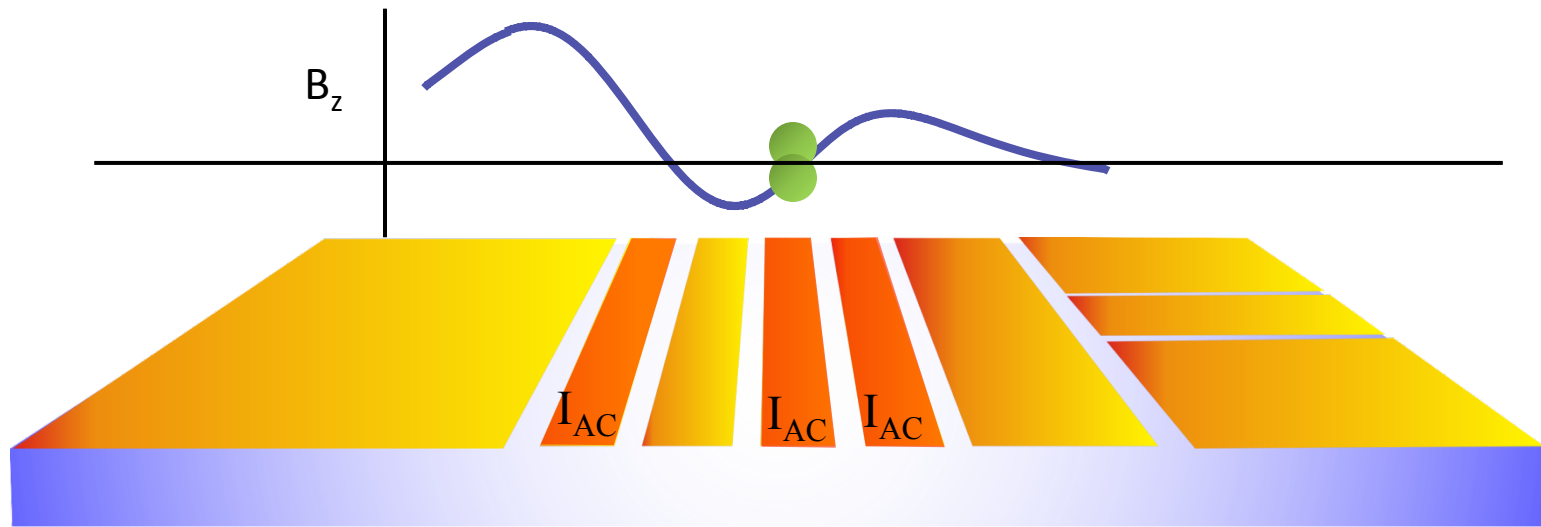
2-qubit (Mølmer-Sørensen) gate ($^{25}\text{Mg}^+$ hyperfine transition)

- $|\downarrow\downarrow\rangle \Rightarrow |\psi\rangle = (1/\sqrt{2})(|\downarrow\downarrow\rangle - i|\uparrow\uparrow\rangle)$
- Generated through application of 2 μW field gradients at $f_0 \pm (f_r + \delta)$



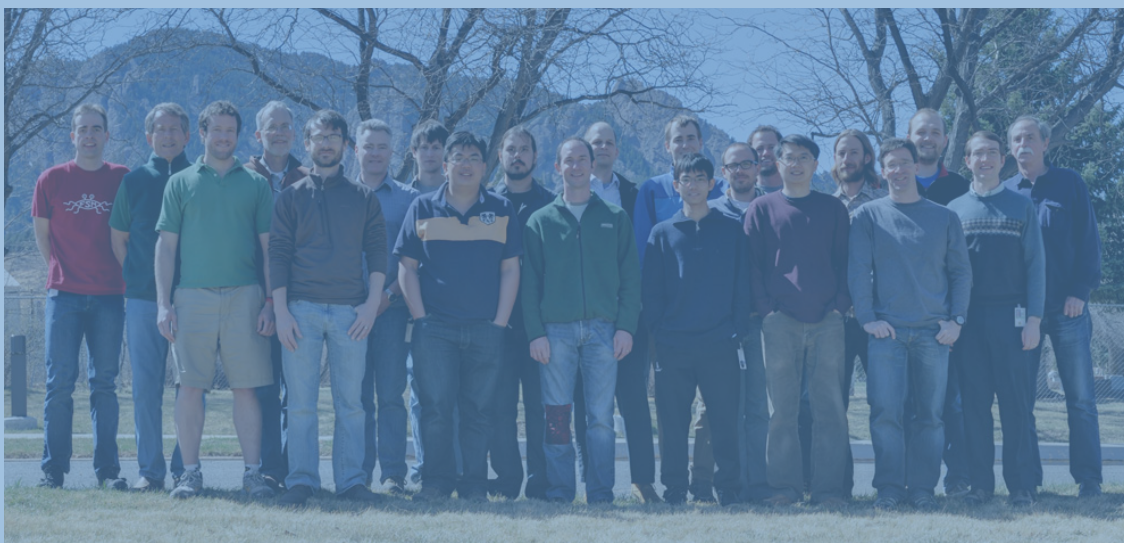
$$\Psi \simeq 1/\sqrt{2} (|\uparrow\uparrow\rangle + e^{i\phi}|\downarrow\downarrow\rangle) \quad F = 0.76(3), T_{\text{gate}} = 200 \mu\text{s}$$

Limits to microwave gate fidelity:



- trap motional frequency stability
 ≈ 1 kHz fluctuation during gate, gate detuning $\delta = 4.9$ kHz
causes: charge fluctuations on trap surface, RF pseudopotential fluctuations
 \Rightarrow cleaner trap surface, employ low-temperature trap
- $B_{osc} \neq 0$ due to μ -wave pulse shape differences between wires
 \Rightarrow AC-Zeeman shift ~ 1 kHz.
 \Rightarrow better pulse shaping, better amplitude stability
- anomalous heating and motional decoherence
heating rate for 2-ion rocking mode < 0.2 quanta/ms, COM ~ 5 quanta/ms
 \Rightarrow low-temperature trap, smaller trap?
- crosstalk !? (single-qubit gates)
 \Rightarrow multizone test trap

Trapped-ion metrology experiments at NIST



Ion Storage
Group
March 23, 2011

Jim Bergquist
Brad Blakestad (now JQI)
John Bollinger
Ryan Bowler
Joe Britton
Kenton Brown
James Chou
Yves Colombe
John Gaebler
David Hanneke (now at Amherst)
Dustin Hite
David Hume (now OFM)
Wayne Itano
Robert Jördens
John Jost
Dietrich Leibfried
Yiheng Lin
Christian Ospelkaus (now U Hannover)
Till Rosenband
Brian Sawyer
Ting-Rei Tan
Mike Thorpe
Ulrich Warring
Andrew Wilson
David Wineland

Quantum Measurement (Ancilla-assisted readout):

- Readout of the Al^+ clock state

Multi-qubit control:

- Entanglement and control with many ions in Penning traps

Entangled States:

- Generation of entangled states with microwave field gradients (novel schemes)
- Coupled ion trap spectroscopy (novel systems and applications)

Theme – Shared ion motion due to strong Coulomb interaction used to generate entanglement and read out quantum states

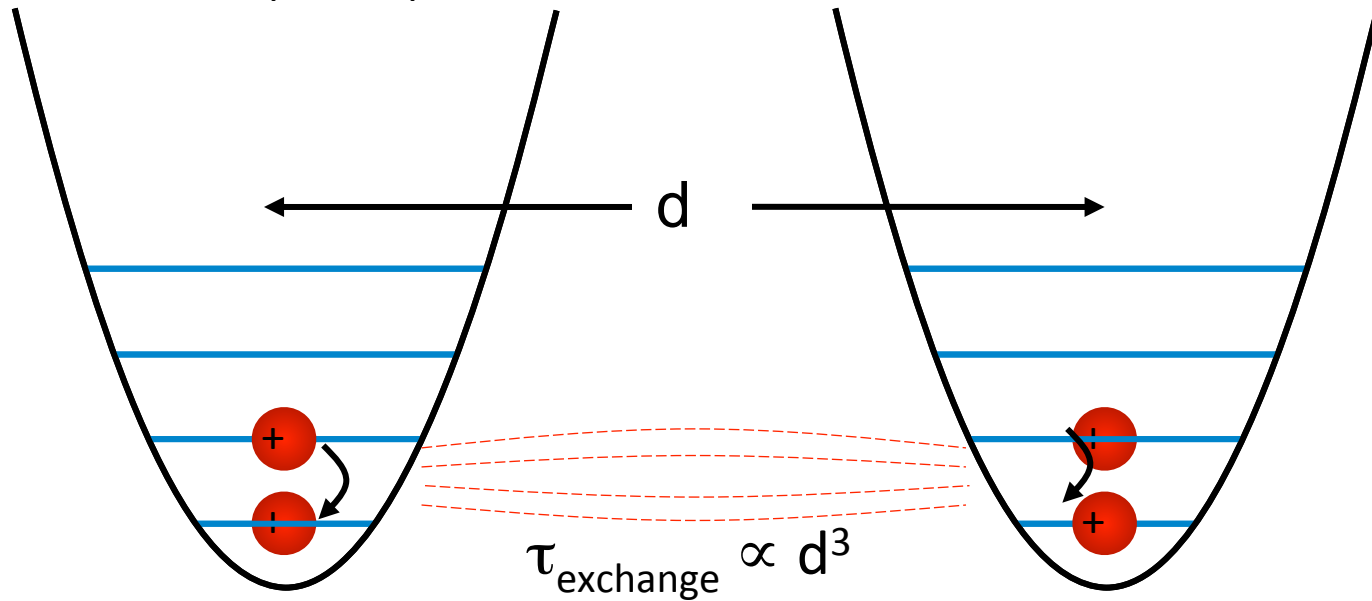


Coupled ion trap spectroscopy

Brown, Ospelkaus, Colombe, Wilson, Leibfried, Wineland, *Nature* **471**, 196 (2011)

see also M. Harlander *et al.*, *Nature*, **471**, 200 (2011)

Can we observe the Coulomb-mediated transfer of a single quantum of motion between ions in separate potential wells?

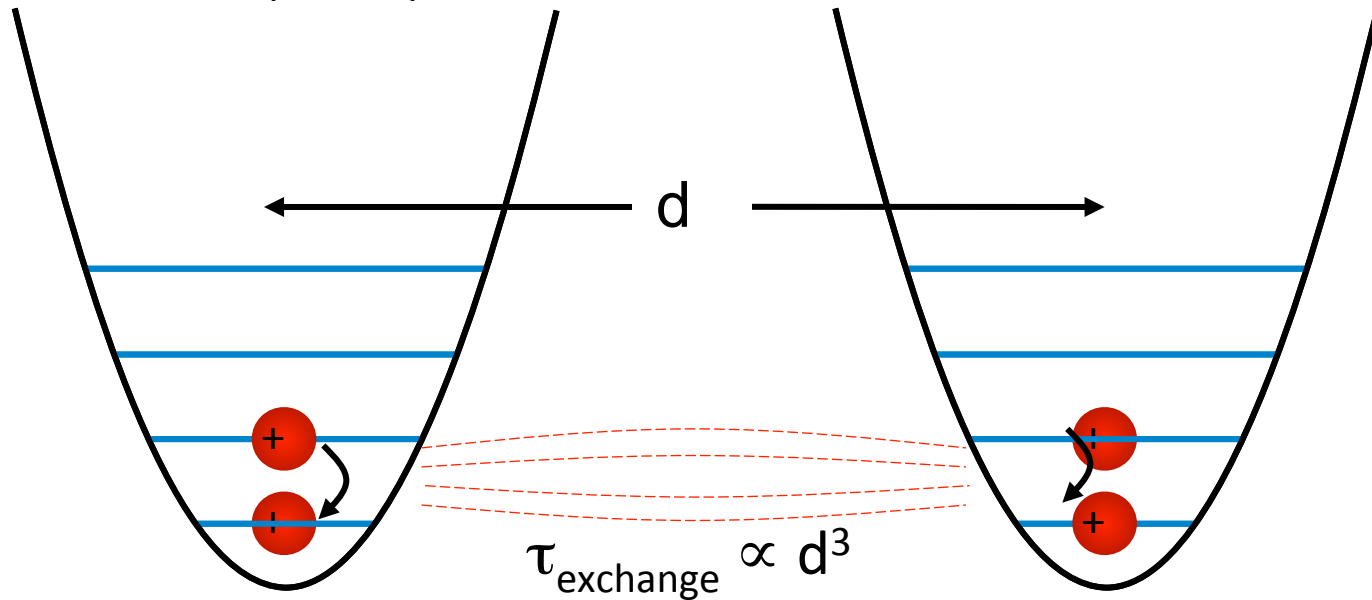


Coupled ion trap spectroscopy

Brown, Ospelkaus, Colombe, Wilson, Leibfried, Wineland, *Nature* **471**, 196 (2011)

see also M. Harlander *et al.*, *Nature*, **471**, 200 (2011)

Can we observe the Coulomb-mediated transfer of a single quantum of motion between ions in separate potential wells?



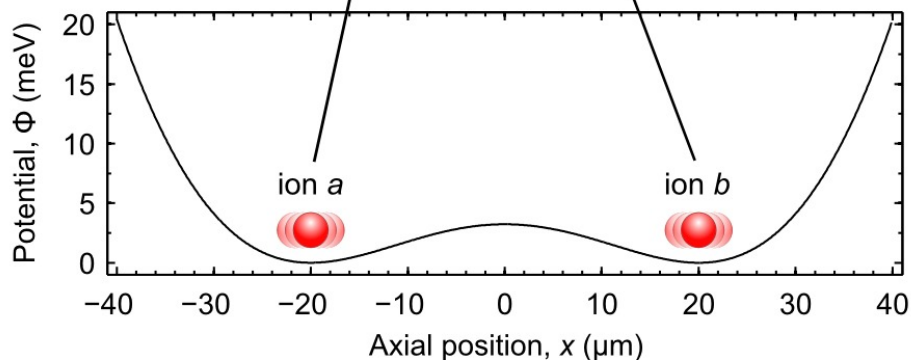
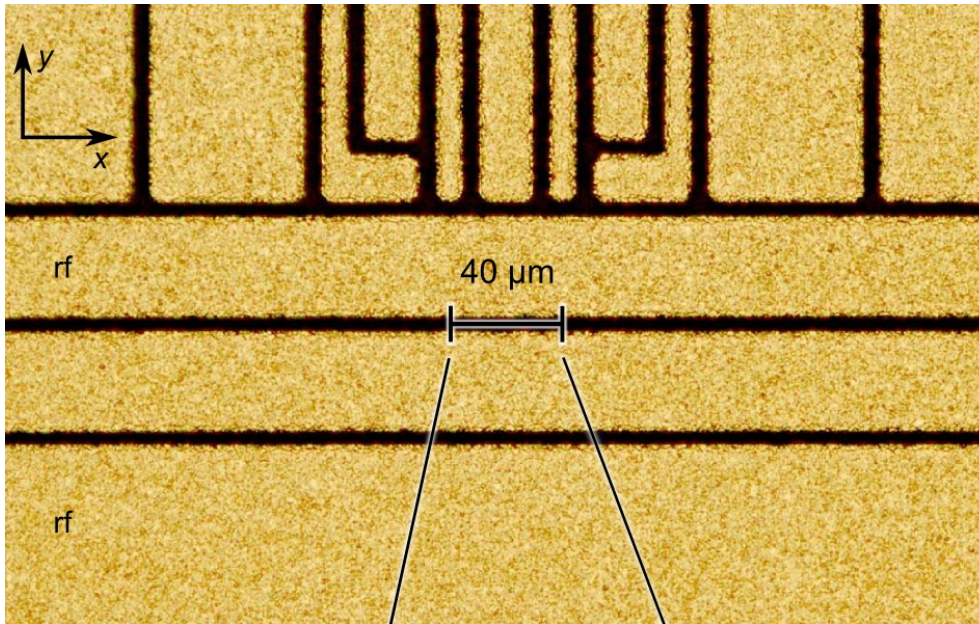
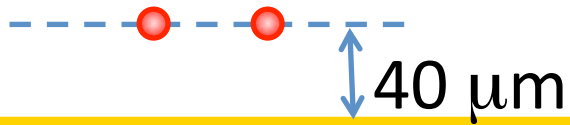
Motivations:

1. extend capabilities of quantum logic spectroscopy (for example between oppositely charged particles or even antimatter particles)
2. potential speed-up of quantum logic operations in a multi-zone quantum information processor
3. first step towards using trapped ions in a hybrid quantum system (i.e. coupling a trapped ion to a quantized mechanical or electrical oscillator)

Coupled ion trap spectroscopy

Brown, Ospelkaus, Colombe, Wilson, Leibfried, Wineland, Nature 471, 196 (2011)

Trap parameters:

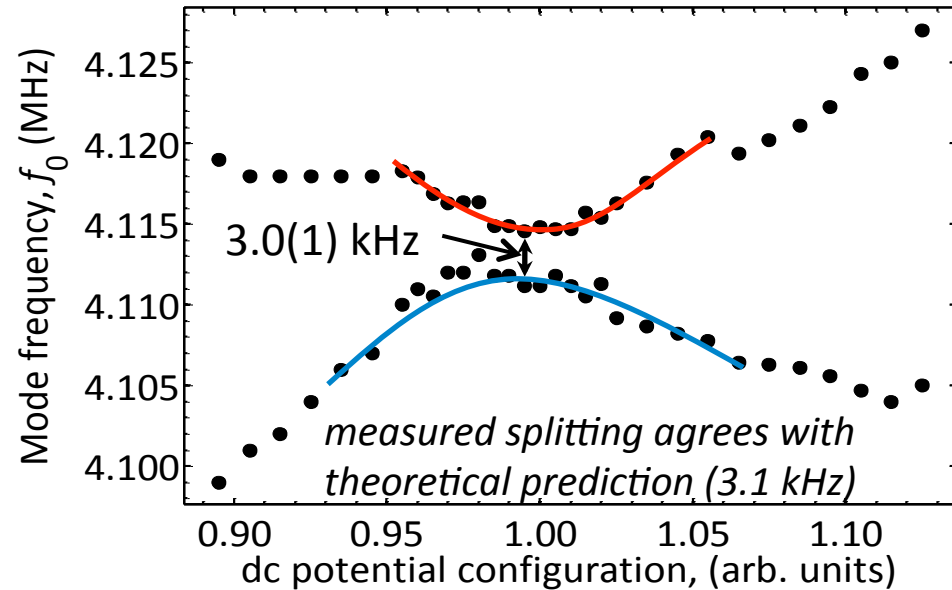


- ${}^9\text{Be}^+$ ions
- $8\ \mu\text{m}$ gold thickness
- $5\ \mu\text{m}$ gaps
- $T \approx 4\ \text{mK}$
- $40\ \mu\text{m}$ ion height
- $40\ \mu\text{m}$ ion separation
- $4\ \text{MHz}$ axial frequency
- Individual control of potentials in both trapping sites

Coupled ion trap spectroscopy

Brown, Ospelkaus, Colombe, Wilson, Leibfried, Wineland, Nature 471, 196 (2011)

**Avoided crossing of
eigenmode frequencies**

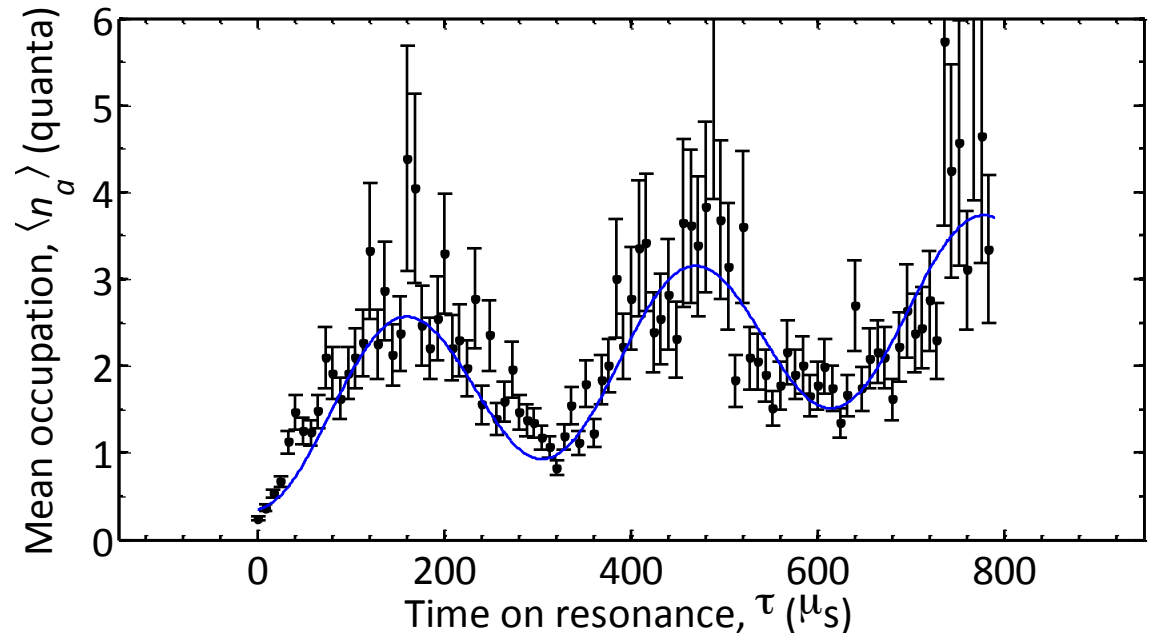


**Coulomb exchange
of a thermal state**

$$\tau_{\text{ex}} = 155 \mu\text{s} \text{ (162 } \mu\text{s predicted)}$$

$$d\langle n \rangle / dt = 1,885 \text{ quanta/s}$$

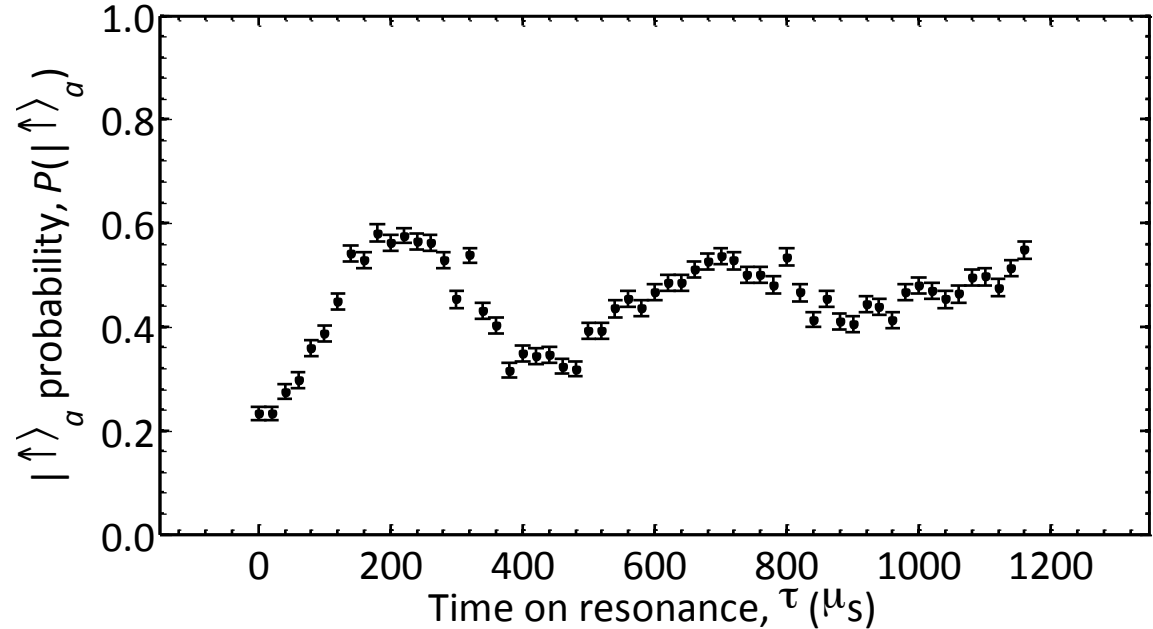
(heating rate)



Coupled ion trap spectroscopy

Brown, Ospelkaus, Colombe, Wilson, Leibfried, Wineland, Nature 471, 196 (2011)

Coulomb exchange of a single quantum



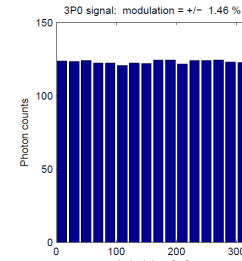
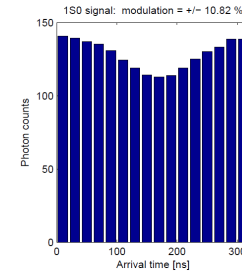
- Initial contrast limited by imperfect state preparation
 - set-up can be improved through better laser polarization, reduced cryostat vibrations, improved laser beam pointing instability, actively control laser
- Decay in contrast is due to motional decoherence
 - heating \rightarrow try a new, cleaner trap
 - trap frequency instability \rightarrow try a new, cleaner trap

Trapped-ion metrology experiments at NIST

Efficient Readout

Ancilla-assisted readout):

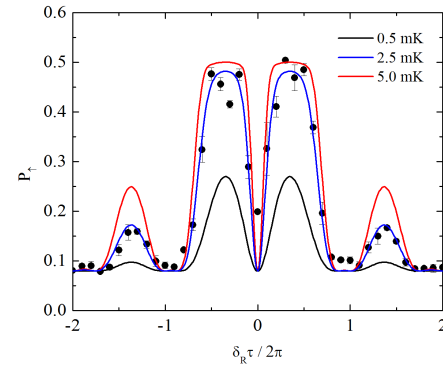
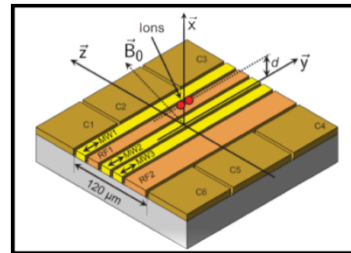
- Readout of the Al^+ clock state



Multi-qubit Control

Multi-qubit control:

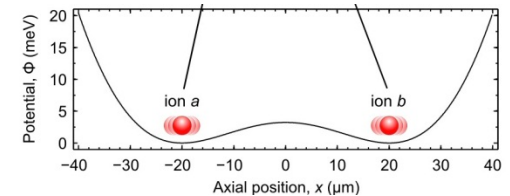
- Entanglement/control with many ions in Penning traps



Entangled States

Entangled States:

- Generation of entangled states with microwave field gradients (novel schemes)



Entangled States:

- Coupled ion trap spectroscopy (novel systems and applications)

Common theme – Shared ion motion due to strong Coulomb interaction used to generate entanglement and read out quantum states